

Subject: Engineering Economics & Costing

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HSSM3204 Engineering Economics & Costing

Module-I: (12 hours)

Engineering Economics – Nature and scope, General concepts on micro & macro economics. The Theory of demand, Demand function, Law of demand and its exceptions, Elasticity of demand, Law of supply and elasticity of supply. Determination of equilibrium price under perfect competition ([Simple numerical problems to be solved](#)). Theory of production, Law of variable proportion, Law of returns to scale.

Module-II: (12 hours)

Time value of money – Simple and compound interest, Cash flow diagram, Principle of economic equivalence. Evaluation of engineering projects – Present worth method, Future worth method, Annual worth method, internal rate of return

method, Cost-benefit analysis in public projects. Depreciation policy, Depreciation of capital assets, Causes of depreciation, Straight line method and declining balance method.

Module-III: (12 hours)

Cost concepts, Elements of costs, Preparation of cost sheet, Segregation of costs into fixed and variable costs. Break-even analysis-Linear approach. (Simple numerical problems to be solved)

Banking: Meaning and functions of commercial banks; functions of Reserve Bank of India. Overview of Indian Financial system.

Text Books:

1. Riggs, Bedworth and Randhwa, “Engineering Economics”, McGraw Hill Education India.
2. D.M. Mithani, Principles of Economics. Himalaya Publishing House

Reference Books :

1. Sasmita Mishra, “Engineering Economics & Costing“, PHI
2. Sullivan and Wicks, “ Engineering Economy”, Pearson
3. R.Paneer Seelvan, “ Engineering Economics”, PHI
4. Gupta, “ Managerial Economics”, TMH
5. Lal and Srivastav, “ Cost Accounting”, TMH

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MODULE - 1 DEMAND AND LAW OF DEMAND

Meaning of Demand

The demand for any commodity, at a given price, is the quantity of it which will be bought per unit, of time at the price. From this definition of demand two things are quite clear:

Firstly, demand always refers to demand at a price. If demand is not related to price, it conveys no sense. To say that the demand for mangoes is 100 kgs. fails to convey any sense. It should be always related to price. Again in the words of Shearman, "To speak of the demand of a commodity in the sense of the mere amount that will be purchased without reference to any price will be meaningless."

Secondly, demand always means demand per unit of time. The time may be a day, a week or a month, etc.

Therefore, “the demand for any commodity or service is the amount that will be bought at any given price per unit of time.”

—G. L. Thirkettle.

There is a difference between ‘desire’ ‘need’ and ‘demand’. A desire “will become demand only if a consumer has the means to buy a thing and also he is prepared to spend the money.. Suppose Ram has the desire of having a fan. But this desire will become demand only if he has 350 rupees and he is prepared to spend this money. Thus by demand -we mean the various quantities of a given commodity or service which -consumers would buy in the market in a given period of time at various prices. According to Pension, “Demand implies, three things (a) desire to possess a thing, (b) mean of purchasing it and (c) willingness to use those means for purchasing it.”

Meaning of Demand Schedule

Demand schedule depicts the “various quantities of a commodity which will be demanded at different prices. Quantity demanded will be different at different prices because with an increase in price, demand falls and with a fall in prices demand extends. Demand schedule can be of the following two types :—

- (i) Individual Demand Schedule.
- (ii) Market Demand Schedule.

Individual Demand Schedule : Individual Demand Schedule shows the various quantities demanded by one person at different prices, individual Demand Schedule can be shown as follows :

Price (In Rupees)	Demand of Mangoes in Kgs
Rs.5	1 Kg.

Rs.4	2 Kgs.
Rs.3	3 Kgs.
Rs.2	4 Kgs.
Rs.1	5 Kgs.

As is clear from the above schedule, the demand for mangoes of a consumer is 1 kg. when the price is 5 rupees per kg. When price falls to; Rs. 4 demand for mangoes extends to 2 kgs. Again demand for mangoes extends to 5 kgs when price is 1 rupee per kg.

Individual Demand Curve. We can show the individual demand schedule with the help of the following diagram.

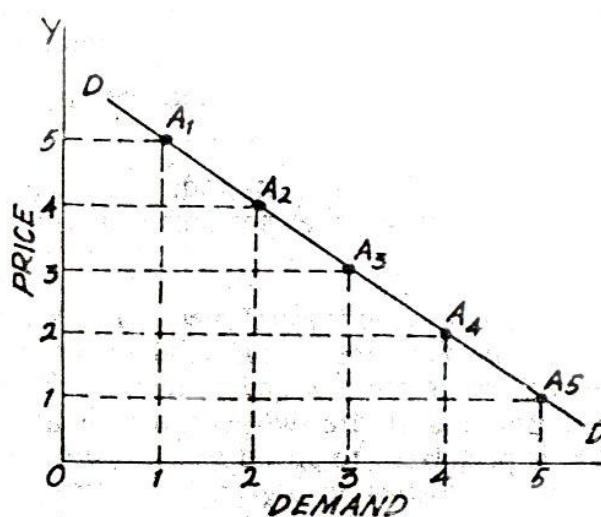


Fig. 4

On OX-axis we measure the quantity demand while on OY-axis we take the price of mangoes per kg. When price is Rs. 5 per kg. demand is 1 kg., likewise when the price is 4 rupees, per kg. demand is 2 kgs., etc. By combining the pts. A₁, A₂, A₃, A₄, A₅, we get the demand curve DD. This is called the individual demand curves.

Market Demand Schedule - If we add up the demand at various prices of all consumers in the market we will get the market demand schedule. Let us suppose there are 3 consumers, A, B & C in the market. If now we add the quantity demanded by A,B and C at different prices, we will get the market demand schedule, it can be shown as follows :

Market Demand Schedule :

Price (Rupees)	Demand of A	Demand of B	Demand of C	Total Demand in the Market (KG)
5 Rs. per kg.	1	3	2	6
4 Rs. per kg.	2	4	3	9
3 Rs. per kg.	3	5	4	12
2 Rs. per kg.	4	6	5	15
1 Rs. per kg.	5	7	6	18

When price is Rs.5/ kg total demand of all consumers is 6kg. When price is Rs.4/- total demand of the consumer is 9kg.

Market Demand curve : Market demand curve can be shown as follows :

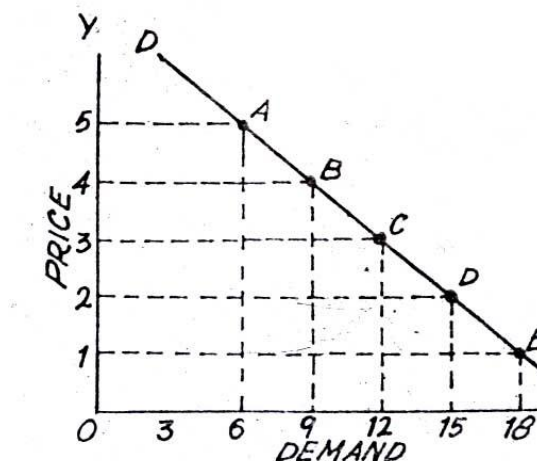


Fig. 5

On OX-axis we take the total quantity demanded of mangoes in the market.

On Y-axis, we measure the prices. When price is Rs.5/- per kg. total quantity

demand 6kg. Again when price is Rs.4/- per kg total quantity demanded goes up to 9 kgs., etc. By combining the points A,B,C,D, and E we get DD. The demand curve market as a whole. Market Demand curve can also be known by adding up the individual demand curves. We assume that there are 2 consumers A and B. If we know the demand curve of A and B we can find our the market curve as follows :

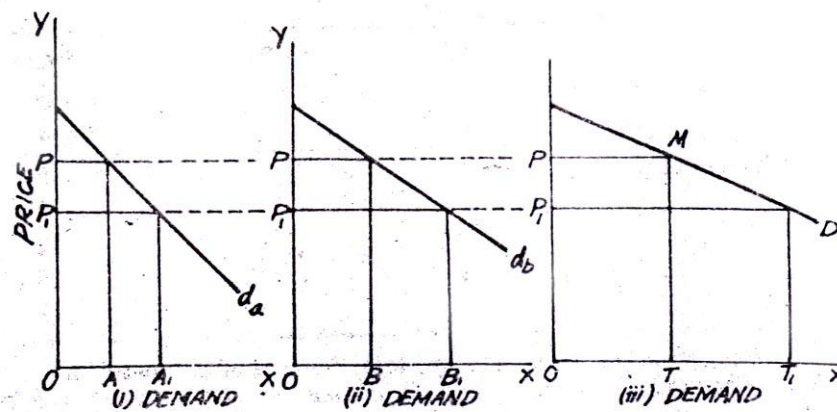


Fig. 6

In the above figures (i), (ii) and (iii) we show the demand of consumer A, consumer B and total demand respectively. On OX-axis we measure demand and OY-axis we measure the price d_a shows the demand curve of consumer 'A' and d_b shows the demand curve of consumer 'B'. At price OP, the quantity demanded by consumer 'A' is OA while the quantity demanded by consumer 'B' at this price is OB. The total demand of consumers 'A' and 'B' shall be $OA+OB$. In diagram (iii) total demand is OT at price OP. Here $OT=OA+OB$. When price falls to OP_1 the quantity demanded increases to OA_1OB_1 in the case of consumers A and B respectively. Now the market demand at price OP_1 shall be equal to OA_1+OB_1 . In figure (iii) the total demand is OT_1 at price OP_1 . Here $OT_1=OA_1+OB_1$. By joining the points M and N, we get Dm which is the market demand curve.

Importance of the Demand Schedule.

1. With the help of demand schedule we can know the approximate changes in demand because of a change in price.
2. We can discuss the Elasticity of the demand with the help of demand/schedule.
3. Law of demand can also be discussed with the help of demand schedule.
4. Price in the market is also determined with the help of demand schedule and supply schedule.
5. Demand schedule is very useful for the business community. With its help, businessman can know as to how much shall be the increase in demand because of a fall in price.

LAW OF DEMAND

Law of demand establishes a relationship between the price and the quantity demanded of a commodity. Other things remaining the same, when the price of a commodity falls its demand will go up likewise when the price of a commodity rises its demand will fall. Price and demand move in opposite directions. There is no proportionate relationship between price and demand. A 10% fall in price will not necessarily lead to a 10% increase in demand.

In the words of Marshall, “The greater the amount to be sold, the smaller must be the price at which it is offered in order that it may find purchasers; or in other words, the amount demanded increases with a fall in price, and diminishes with a rise in price”.

According to *Samuelson*, “When the price of a good is raised, less of it will be demanded. People will buy more at lower price and buy-less at higher prices.”

According to Meyers, “People demand a larger quantity of goods and services only at a lower price than at a higher price.”

In simple words law of demand states that, other thing being equal, more will be demanded at lower, prices than at higher prices.

Law of demand can be shown with the help of the following table :

Price of Apples (Paisa)	Demand for Apples (Unit)
50	2
40	4
30	6
20	8
10	10

When price is 30 Paise, consumer demand is 6 apples. When price falls to 20 Paise, he demands 8 apples and when price goes to 40 Paise he demands 4 apples. Thus when price falls, demand expands and -when price rises, demand contracts.

Law of demand can - be shown with the help of the following diagram:

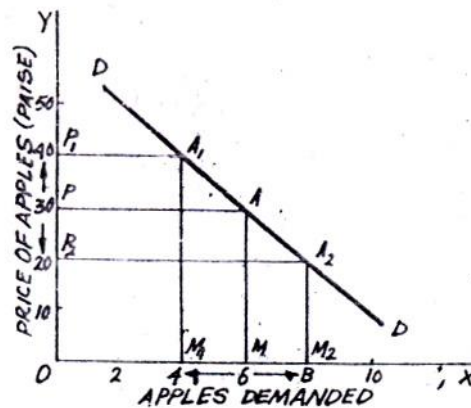


Fig. 7

We see that at OP price our demand increases to OP_1 the demand falls to OM_1 . When the price falls to OP_2 the demand increases to OM_2 .

Causes : The law applies because of the following reasons

1. Law of Diminishing Marginal Utility : It is quite natural that when a person continues buying large number pf units of the same commodity, its marginal utility will progressively fall. On the other hand when the stock of a commodity goes on falling; then its-marginal utility will progressively rise. We also know that marginal utility is measured by price. When a person purchases less amount of a commodity then the marginal utility of that commodity will be high for him and he will be ready to pay more price and vice versa. So we come to the conclusion that people purchase more at a low price and less at high price.

2. Income Effect : When price falls, real income of the consumer rises. He is therefore, in a position to purchase more units of commodity. When the price rises, real income of the consumer falls and he purchases less units of a commodity.

3. Substitution effect : When the price of one commodity falls people will purchase more of that commodity. When the price of one commodity rises people will purchase less of that commodity. The substitution effect of a price reduction is always positive and hence larger quantities will be bought at lower prices.

Assumptions of the Law :

The Law of Demand is based on the following assumptions :

1. Income of the buyer remains the same.
2. The taste of the buyer remains the same.
3. The prices of other goods—substitutes and complements— remain unchanged.
4. No close substitute is discovered.
5. There is no 'prestige value' for the product in question. Only when these conditions are assumed constant, the Law of Demand will operate. In other words, the tastes, incomes and the prices of substitutes and complements are main determinants of price relationship. Hence I they are assumed constant.

Limitations of the Law/Exception to Law of Demand

1. Change in Habit, Customs and Income : Law of Demand tells us that demand goes up with a fall in price and goes down with a rise in price. But an increase in price will bring down the demand if at the same time the income of the consumer has also increased.

2. *Necessaries of Life* : Law of Demand is not applicable in the case of necessities of life also. An increase in the price of flour will not bring down its demand. Likewise a fall in its price will not very much increase the demand for it.

3. *Fear of Shortage in Future* : If there is a fear of shortage of a commodity in future its demand will increase in the present as people would start storing it. 'But according to the Law of Demand its demand should go up only when its price falls.

4. *Fear of a Rise in Prices in Future* : Similarly if the people think that the price of a particular, ^commodity will increase in future, they will store it. In other words, the demand of that commodity shall increase at the same price. But the Law of Demand states that demand should go up only if price will lower the demand.

5. *Articles of Distinction* : This law does not hold good in case of those commodities which confer, social distinction. When the price of such commodities goes up, their demand shall also increase. For .example, an increase in the price of demand will raise its demand and a fall in price will lower the demand.

***Giffin Goods* :** Sir Robert Giffin observed that sometimes people buy less of a good at a lower price and more of a good at a higher price. He cited the example of low-paid British wage-earners. During the early period of the nineteenth century, a rise in the price of bread as before. Hence, all such inferior goods are known as Giffin Goods and they are considered to be an exception to the Law of Demand.

***Ignorance* :** It is possible that a consumer may not be aware of the previous price of a commodity. In this case he might start purchasing more of a commodity when its price has actually gone up.

PRICE ELASTICITY OF DEMAND

We have discussed in previous chapters that when the price of a good falls, its quantity demanded rises and when the price of the good rises, its quantity demanded falls. This is generally known as law of demand. This law of demand indicates only the direction of change in quantity demanded in response to a change in price. This does not tell us by how much or to what extent the quantity demanded of a good will change in response to a change in its price. This information as to how much or to what extent the quantity demanded of a good will change as a result of a change in its price is provided by the concept of elasticity of demand. The concept of elasticity has a very great importance in economic theory as well as in engineering economics.

VARIOUS CONCEPTS OF DEMAND ELASTICITY

It is price elasticity of demand which is usually referred to as elasticity of demand. But, besides price elasticity of demand, there are various other concepts of demand elasticity. As we have seen in earlier chapters that demand for a food is determined by its price, incomes of the people, prices of related goods, etc. Quantity demanded of a good will change as a result of a change in the size of any of these determinants of demand. The concept of elasticity of demand therefore refers to the degree of responsiveness of quantity demanded of a good to a change in its price, income or prices of related goods. Accordingly, there are three kinds of demand elasticity : price elasticity, income elasticity, and cross elasticity. Price elasticity of demand relates to the responsiveness of quantity demanded of a good to the change in its price. Income elasticity of demand refers to the sensitiveness of quantity demanded to the change in income. Cross elasticity of demand means the degree of responsiveness of demand of a good to a change in the price of a

related good, which may be either a substitute for it or a complementary with it. Besides these three kinds of elasticities there is another type of elasticity of demand called elasticity of substitution which refers to the change in quantity demanded of a good in response to the change in its relative price alone, real income of the individual remaining the same.

PRICE ELASTICITY OF DEMAND

Price elasticity means the degree of responsiveness or sensitiveness of quantity demanded of a good to changes in its prices. In other words, price elasticity of demand is a measure of the relative change in quantity purchased of a good in response to a relative change in its price. Price elasticity can be precisely defined as “the proportionate change in quantity demanded in response to a small change in price, divided by the proportionate change in price”. Thus,

$$\begin{aligned} \text{Price Elasticity} &= \frac{\text{Proportionate change in quantity demanded}}{\text{Proportionate change in price}} \\ &= \frac{\frac{\text{Change in quantity demanded}}{\text{Quantity demanded}}}{\frac{\text{Change in Price}}{\text{Price}}} \end{aligned}$$

or, in symbolic terms

$$\begin{aligned} e_p &= \frac{\frac{\Delta q}{q}}{\frac{\Delta p}{p}} = \frac{\Delta q}{q} \div \frac{\Delta p}{p} \\ &= \frac{\Delta q}{q} \times \frac{p}{\Delta p} \\ &= \frac{\Delta q}{\Delta p} \times \frac{p}{q} \end{aligned}$$

where, e_p stands for price elasticity
 q stands for quantity
 p stands price
 Δ stands for infinitesimal change.

Mathematically speaking, price elasticity of demand (e_p) is negative, since the change- in quantity demanded is in opposite direction to the change in price. When price falls, quantity demanded rises and vice versa. But for the sake of convenience in understanding the magnitude of response of quantity demanded to the change in price we ignore the negative sign and take into account only the numerical value of the elasticity. Thus if 2% change in price leads to 4% change in quantity demanded of good A and 8% change in that of B, then the above formula of elasticity will give the value of price elasticity of good A equal to 2 and of good B equal to 4. It indicates that the quantity demanded of good B changes much more than that of good A in response to a given change in price. But if we had written minus signs before the numerical values of elasticities of two goods, that is, if we had written the elasticities as -2 and -4 respectively as strict mathematics would require us to do, then since -4 is smaller than -2 , we would have been misled in concluding that price elasticity of demand of B is less than that of A.

Types of price elasticity

Different products react differently to the price change. A price change for a essential product such as rice has little impact on demand while the price change in other products has huge impact on demand. This gives rise to the different types of price elasticities. Price elasticities are generally classified into the following categories.

- Perfectly elastic demand
- Absolutely inelastic demand or perfectly inelastic demand
- Unit elasticity of demand
- Relatively elastic demand
- Relatively inelastic demand

1. Perfectly elastic demand ($e_p = \infty$)

Here there is no need for reduction in price to cause an increase in demand, for this to be the case, a firm can sell all the quantity it wants at the prevailing price, but the firm can sell none at all at even a slightly higher price. Here the demand curve is horizontal.

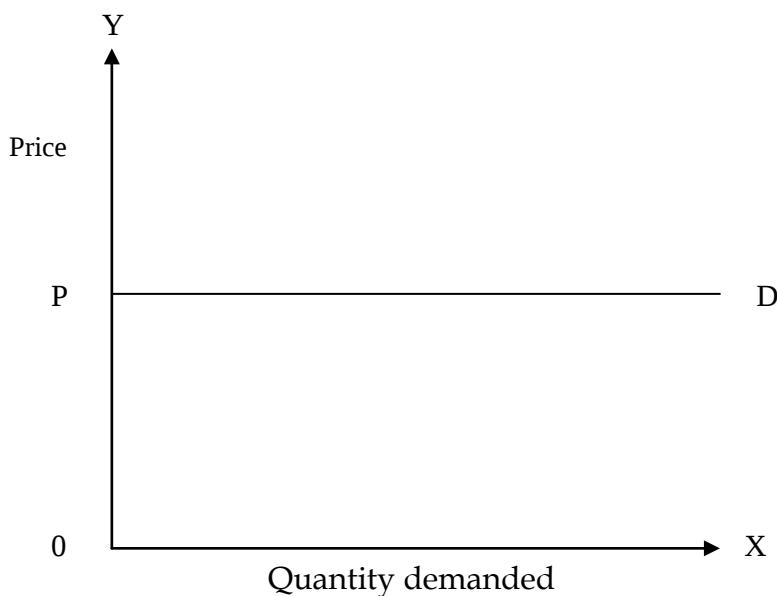


Fig. 8 : Perfectly elastic demand curve

2. Absolutely inelastic demand or perfectly inelastic demand ($e_p=0$) :

Absolutely inelastic demand is where a change in price however large, causes no change in the quantity demanded of a product. Here, the shape of the demand curve is vertical. Some examples of absolutely inelastic demand

are the demand of essential commodities such as rice, wheat etc. whose change in price does not affect the quantity demanded.

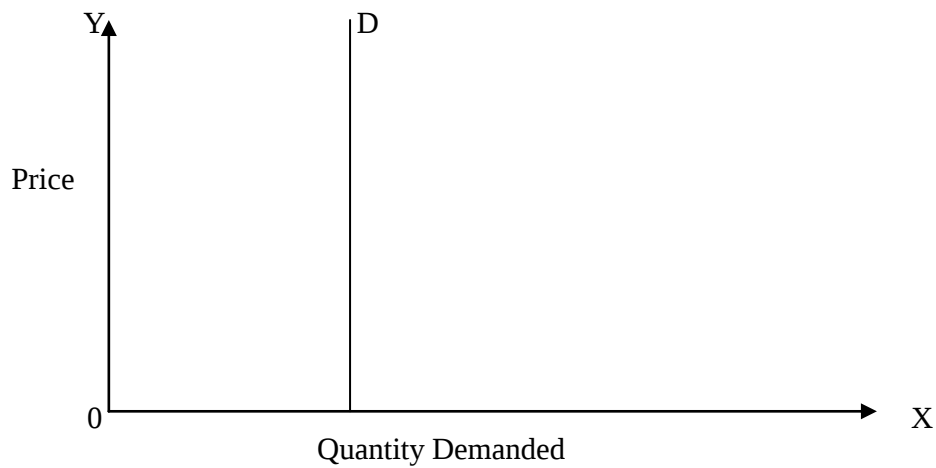


Fig. 9 : Absolutely inelastic demand

3. Unit elasticity of demand ($e_p = 1$) :

Unit elasticity is where a given proportionate change in price causes an equal proportionate change in the quantity demanded of the product. The shape of the demand curve here is that of a rectangular hyperbola.

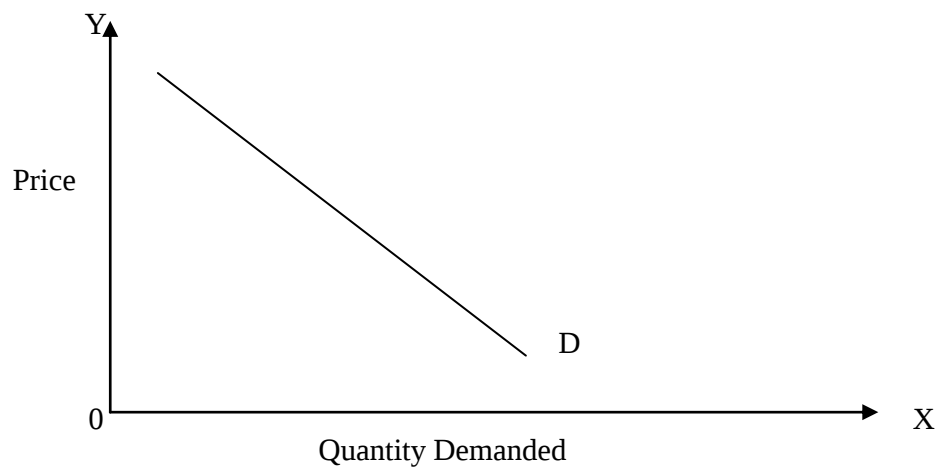


Figure 10 : Unit Elasticity of Demand

4. Relatively Elastic of Demand ($e_p > 1$) :

It is where a reduction in price leads to more than proportionate change demand. Here the shape of the demand curve is flat.

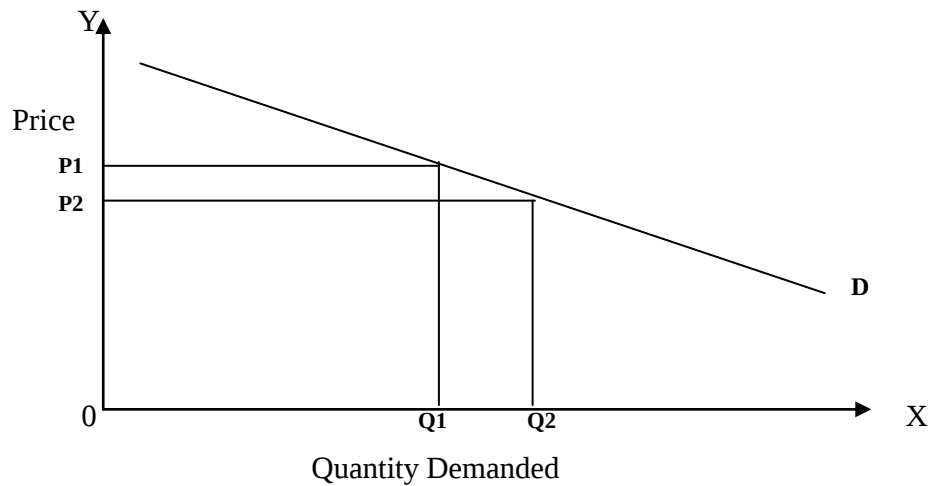


Fig. 11 : Relatively elastic of demand

5. Relatively in elastic demand ($e_p < 1$) :

It is where a decline in price leads to less than proportionate increase in demand. Here the shape of the demand curve is steep.

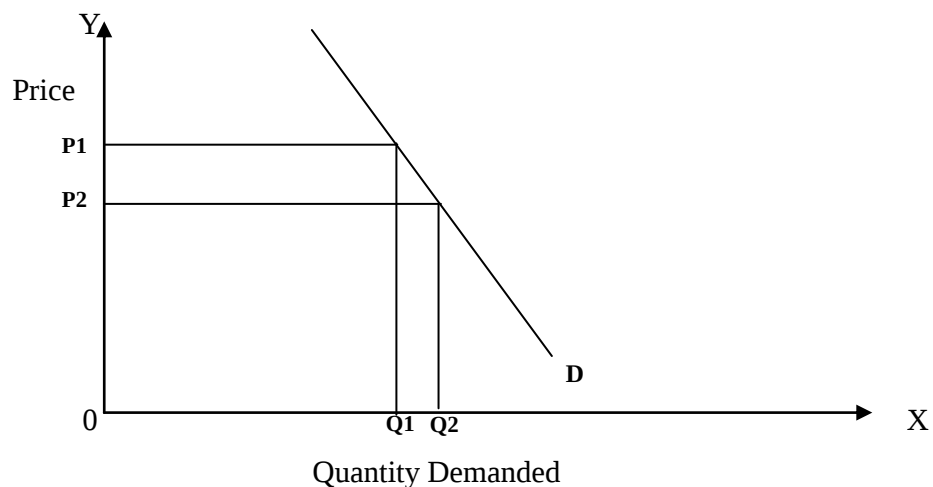


Figure 12 : Relatively in elastic of demand

Factors determining price elasticity of Demand:

The elasticity of demand depends on the following factors namely

1. Nature of the product
2. Extent of usage
3. Availability of substitutes
4. Income level of people
5. Proportion of the income spent of the product
6. Urgency of demand and
7. Durability of a product.

Let us have a brief explanation of these points

1. Nature of the product

The demand for products that fall in the category of necessities (eg. Rice, salt, wheat etc) are usually inelastic. This is because their demand do not change even when there is a change in price. On the other hand the demand for luxuries (TV's, washing machines etc) are elastic where even a small change in price reflects on a huge change in the demand

2. Extent of usage:

If a product has varied usage (eg. steel, aluminums, wood etc) then it has a comparatively elastic demand. For example, if the price of teak wood falls then its usage in many areas will be increased and the opposite happens when the price rises, the usage in some quarters will be cut down while the usage in other and will be the same.

3. Availability of substitutes:

When a product has many substitutes then its demand will be relatively elastic. This is because if the price of one substitute goes down then customers switch to that substitute and vice versa. Products without substitutes or has weak substitutes have relatively inelastic demand.

4. Income level of people:

People with high income are less affected by price changes in products while people with low income, are highly affected by price rise. People with high income will not change their buying habits because of the increase in price of either essential commodities or luxuries while other will cut back on purchase of certain commodities to compensate for the essential commodities if there is a price increase.

5. Proportion of income spent on the commodity:

When a person spends only a very small part of his income on certain products (match boxes, salt etc) the price change in these products does not materially affect his demand for the product. Here the demand is inelastic.

6. Urgency of Demand:

If a person requires buying a product immediately no matter what or no other go but to-buy a product at that point of time, with no substitutes, the demand for that product becomes inelastic. For example if one is building a lodge and is in urgent need for completing the construction then, any price change in cement or bricks or steel etc will have little impact on the demand for those products.

THEORY OF PRODUCTION

The act of production involves the transformation of inputs into outputs. The word production in economics is not merely confined to effecting physical transformation in the matter, "It also covers the rendering of services such as transporting, financing, wholesaling and retailing. Laws of production, or in other words, the generalizations regarding relations between inputs and outputs developed in the chapter will apply to all these types of production.

The relation between inputs and output of a firm has been called the 'Production Function'. Thus the theory of production is the study of the production function. The production function of a firm can be studied by holding the quantities of some factors fixed, while varying the amount of other factors. This is done when the law of variable proportions is derived. The production function of a firm can also be studied by varying the amounts of all factors. The behaviour of production when all factors are varied is the subject matter of the laws of returns to scale. Thus, in the theory of production, the study of (a) the law of variable proportions and (b) the laws of returns to scale is included.

IMPORTANCE OF THE THEORY OF PRODUCTION

The theory of production plays a double role in the price theory. Firstly, it provides a basis for the analysis of relation between costs and amount of output. Costs govern supply of a product which, together with demand, determines the price of a product. The prices of inputs or factors of production influence the costs of production and hence play a part in determining the prices of products. Secondly, the theory of production provides a basis for theory of firm's demand for factors (inputs) of production. Demand for factors of production or inputs, together with the supply of them, determines their prices.

The theory of production is relevant to the macro-theory of distribution. The aggregate distributive shares of the various factors, for instance, aggregative shares of wages and profits in national income, depend upon the elasticity of substitution between factors which is an important concept of the theory of production. In fact, in the neo-classical macro-theory of -distribution, elasticity of substitution is the crucial factor which determines the aggregative shares of the various factors.

Before we take up the explanation of the theory of production in detail, we shall first explain the concept of 'Equal-Product Curve' which is the tool of analysis in the theory of production.

EQUAL-PRODUCT CURVES OR ISOQUANTS

Equal-product curves are similar to the indifference curves of the theory of consumer's behaviour. An equal-product curve represents all those input combinations which are capable of producing the same level of output. The equal-product curves are thus contour lines which trace the loci of equal outputs. These equal-product curves are also known as isoquants (meaning equal quantities) and iso-product curves. Since an equal-product curve represents those combinations of inputs which will be capable of producing an equal quantity of output, the producer would be indifferent between them as such. Therefore, another name which is often given to the equal-product curves is production-indifference curve'.

The concept of equal-product curves can be easily understood from Table 1. It is presumed that two factors X and Y are being employed to produce a product.

TABLE -1

Various Factor Combinations to Produce a given level of Output

Factor Combination	Factor X	Factor Y
A	1	12
B	2	8
C	3	5
D	4	3
E	5	2

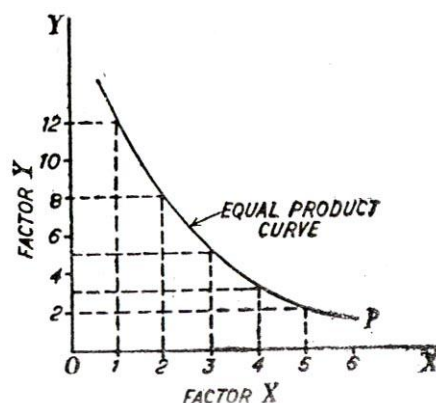


Fig. 1

Each of the factor combinations A, B, C, D and E produces the same level of output, say, 20 units. To start with, factor combination A consisting of 1 unit of factor X and 12 units of factor Y produces the given 20 units of output. Similarly, combination B consisting of 2 units of X and 8 units of Y, combination C consisting of 3 units of X and 5 units of Y, combination D consisting of 4 units of X and 3 units of Y, and combination E consisting of 5 units of X and 2 units of Y are capable of producing the same amount of output, we have plotted all these combinations and by joining them we obtain the equal-product curve showing that every combination represented on it can produce 20 units of output.

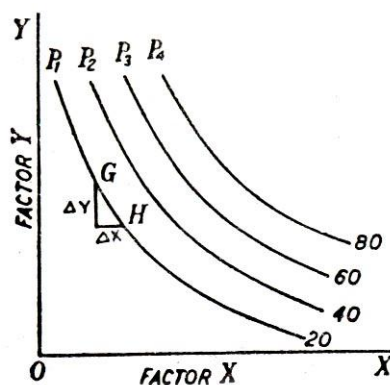


Fig. 2

Though equal product curves are similar to the indifference curves of the theory of consumer's behaviour, yet there is one important difference between the two. An indifference curve represents all those combinations of two goods which provide the same satisfaction or utility to a consumer but no attempt is made to specify the level of satisfaction or utility it stands for. This is so because the measurement of satisfaction or utility in unambiguous terms is not possible. That is why we usually label indifference curves by ordinal numbers as I, II, III, etc., indicating that a higher indifference curve represents a higher level of satisfaction than a lower one, but the information as to by how much one level of satisfaction is greater than another is not provided. On the other hand, we can label equal product curves in the physical units of output without any difficulty. Production of a good being a physical phenomenon lends itself easily to absolute measurement in physical units. Since each equal product curve represents specified level of production, it is possible to say by how much one equal-product curve indicates greater or less production than another. In Fig. 2 we have drawn an equal-product map or isoquant map with a set of four equal product curves which represent 20 units, 40 units, 60 units and 80 units of output respectively. Then, from this set of equal-product curves it is very easy to judge by how much production level on one equal-product curve is greater or less than on another.

MARGINAL RATE OF TECHNICAL SUBSTITUTION

Marginal rate of technical substitution in the theory of production is similar to the concept of marginal rate of substitution in the indifference curve analysis of consumer's demand. Marginal rate of technical substitution indicates the rate at which factors can be substituted at the margin without altering the level of output. More precisely, marginal rate of technical substitution of factor X for factor Y may be defined as the amount of factor Y which can be replaced by one unit of factor X, the level of output remaining unchanged.

The concept of marginal rate of technical substitution can be easily understood from the Table 2.

Each of the input combinations A, B, C, D and E yields the same level of output. Moving down the table from combination A to combination B, 4 units of Y are replaced by 1 unit of X in the production process without any change in the level of output.

TABLE 2
Marginal Rate of Technical Substitution

Factor Combinations	Factor X	Factor Y	MRTS of X for Y
A	1	12	4
B	2	8	3
C	3	5	2
D	4	3	1
E	5	2	

Therefore, the marginal rate of technical substitution is 4 at this stage switching from input combination B to input combination G involves the replacement of 3 units of factor Y by an additional unit of factor X, output remaining the same. Thus, the marginal rate of technical substitution is now 3. Likewise, marginal rate of technical substitution between factor combinations G and D is 2, and between factor combinations D and E is 1.

The marginal rate of technical substitution at a point on the equal product curve can be known from the slope of the equal product curve at that point. Consider a small movement down the equal product curve P_1 from G to H in Fig 2 where a small amount of factor Y, say ΔY , is replaced by an amount of factor X, say ΔX without any loss of output. The slope of the isoproduct curve

P_1 at point G is therefore equal to $\frac{\Delta Y}{\Delta X}$. Thus, marginal rate of technical substitution = slope = $\frac{\Delta Y}{\Delta X}$.

Slope of the equal product curve at a point and hence the marginal rate of technical substitution (MRTS) can also be known by the slope of the tangent drawn on the equal product curve at that point. In Fig 3 the tangent TT' is drawn at point K on the given equal product curve P. The slope of the tangent TT' is equal to $\frac{OT}{OT'}$. Therefore, the

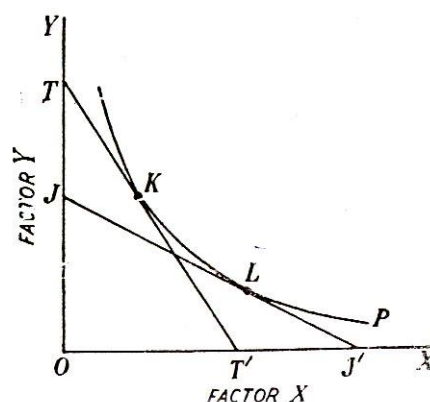


Fig. 3

marginal rate of technical substitution at point K on the equal product curve P is equal to $\frac{OT}{OT'}$. JJ' is the tangent to point L on the equal product curve P. Therefore, the marginal rate of technical substitution at point L is equal to OJ/OJ'.

An important point to be noted about the marginal rate of technical substitution is that it is equal to the ratio of the marginal physical products of two factors. Since, by definition, output remains constant on the equal product curve the loss in physical output from a small reduction in factor Y will be equal to the gain in physical output from a small increment in factor X. The loss in output is equal to the marginal physical product of factor Y (MPV) multiplied by the amount of reduction in Y. The gain in output is equal to the marginal physical product of factor X (MPX) multiplied by the increment in X.

Accordingly,

Loss of output = gain in output

$$\Delta Y \times MP_y = \Delta X \times MP_x$$

$$\frac{\Delta Y}{\Delta X} = \frac{MP_x}{MP_y}$$

But $\frac{\Delta Y}{\Delta X}$, by definition, is the marginal rate of technical substitution of factor X for factor Y.

$$\therefore MRTS_y = \frac{MP_x}{MP_y}$$

We thus see that marginal rate of technical substitution of factor X for factor Y is the ratio of marginal physical productivities of the two factors.

Diminishing Marginal Rate of Technical Substitution.

An important characteristic of marginal rate of technical substitution is that it diminishes as more and more of factor Y is substituted by factor X. In other words, as the quantity of factor X is increased and the quantity of factor Y is reduced, the amount of factor Y that is required to be replaced by an additional unit of factor X so as to keep the output constant will diminish. This is known as the Principle of Diminishing Marginal Rate of Technical Substitution. This principle of diminishing marginal rate of technical substitution is merely an extension of the Law of Diminishing Returns to the relation between the marginal physical productivities of the two factors. Along an equal product curve, as the quantity of factor X is increased and the quantity of factor Y is reduced, the marginal physical productivity of X diminishes and the marginal physical productivity of Y increases. Therefore, less and less of factor Y is required to be substituted by an additional unit of X so as to maintain the same level of output.

It may also be noted that the rate at which the marginal rate of technical substitution diminishes is a measure of the extent to which the two factors can

be substituted for each other. The smaller the rate at which the marginal rate of technical substitution diminishes, the greater the substitutability between the two factors. If the marginal rate of substitution between any two factors does not diminish and remains constant, the two factors are perfect substitutes of each other.

PROPERTIES OF ISOQUANTS OR EQUAL PRODUCT CURVES

The following are the important properties of equal product curves.

1. *Isoquants, like indifference curves, slope downward from left to right (i.e., they have a negative slope).* This is so because when the quantity of factor X is increased, the quantity of factor Y must be reduced so as to keep output constant.
2. *No two equal product curves can intersect each other.* If the two equal product curves, one corresponding to 20 units of output and the other to 30 units of output intersect each other, there will then be a common factor combination corresponding to the point of intersection. It means that the same factor combination which can produce 20 units of output according to one equal product curves can produce 30 units of output according to the other equal product curve. But this is quite absurd. How can the same factor combination produce two different levels of output, techniques of production remaining unchanged.
3. *Isoquants, like indifference curves, are convex to the origin.* The convexity of equal product curves means that as we move down the curve less and less of factor Y is required to be substituted by a given increment of factor X so as to keep the level of output unchanged. Thus, the convexity of equal product curves is due to the diminishing marginal rate of technical substitution. If the equal product curves were concave to the origin, it would mean that the marginal rate of technical substitution increased as more and more of factor Y was replaced by factor X. This could be valid if

the law of increasing returns applied. Since it is the law of diminishing returns which is more true of the real world, the principle of diminishing marginal rate of technical substitution generally holds good and it makes the equal product curves convex to the origin.

LAW OF VARIABLE PROPORTIONS

Law of variable proportions occupies an important place in economic theory. This law examines the production function with one factor variable, keeping the quantities of other factors fixed. In other words, it refers to the input-output relation when the output is increased by varying the quantity of one input. When the quantity of one factor is varied, keeping the quantity of the other factors constant, the proportion between the variable factor and the fixed factor is altered; the ratio of employment of the variable factor to that of the fixed factor goes on increasing as the quantity of the variable factor is increased. Since under this law we study the effects on output of variations in factor proportions, this is known as the law of variable proportions. The law of variable proportions is the new name for the famous “Law of Diminishing Returns” of classical economics. This law has played a vital role in the history of economic thought and occupies an equally important place in modern economic theory and has been supported by the empirical evidence about the real world. The law of variable proportions or diminishing returns has been stated by various economists in the following manner :

“As equal increments of one input are added; the inputs of other productive services being held constant, beyond a certain point the resulting increments of product will decrease, i.e. the marginal products will diminish” (G. Stigler).

“As the proportion of one factor in a combination of factors is increased, after a point, first the marginal and then the average product of that factor will diminish.” (F. Benham).

“An increase in some inputs relative to other fixed inputs will, in a given state of technology, cause output to increase; but after a point the extra output resulting from the same additions of extra inputs will become less and less.” (P.A. Samuelson).

Marshall discussed the law of diminishing returns in relation to agriculture. He defines the law as follows; “An increase in the capital and labour applied in the cultivation of land causes in general a less than proportionate increase in the amount of product raised unless it happen to coincide with an improvement the arts of agriculture”.

Assumptions of the Law of Variable Proportions. The law of variable proportions (or diminishing returns) as stated above holds good under the following conditions :

1. Firstly, the state of technology is assumed to be given and unchanged. If there is improvement in technology, then marginal and average product may rise instead of diminishing.
2. Secondly, there must be some inputs whose quantity is kept fixed. It is only in this way that we can alter the factor proportions and know its effects on output. This law does not apply in case all factors are proportionately varied. Behaviour of output as a result of the variations in all inputs is discussed under “returns to scale”.
3. Thirdly, the law is based upon the possibility of varying the proportions in which the various factors can be combined to produce a product. The law does not apply to those cases where the factors must be used in fixed proportions to yield a product. When the various factors are required to be used in rigidly fixed proportions, then the increase in one factor would not lead to any increase in output, that is, the marginal product of the factor will then be zero and not diminishing. It may however be pointed

out that products requiring fixed proportions of factors are quite uncommon. Thus the law of variable proportions applies to most of the cases of production.

Three Stages of the Law of Variable Proportions

The varying quantity of one factor combined with a fixed quantity of the other can be divided into three distinct stages. In order to understand these three stages it is better to graphically illustrate the production function with one factor variable. This is done in Fig.4. In this figure, on the X-axis is the quantity of the variable factor and on the Y axis are the total, average and the marginal product. How the total product, average product and marginal product of the variable factor change as a result of the increase in its quantity, that is, by increasing the quantity of one factor to a fixed quantity of the others will be seen in Fig. 4. The total product curve TP goes on increasing to a point and after that it starts declining. Average and marginal product curves also rise and then decline; marginal product curve starts declining earlier than the average product curve. The behaviour of these total, average and marginal products of the variable factor consequent on the increase in its amount is generally divided into three stages which are explained below.

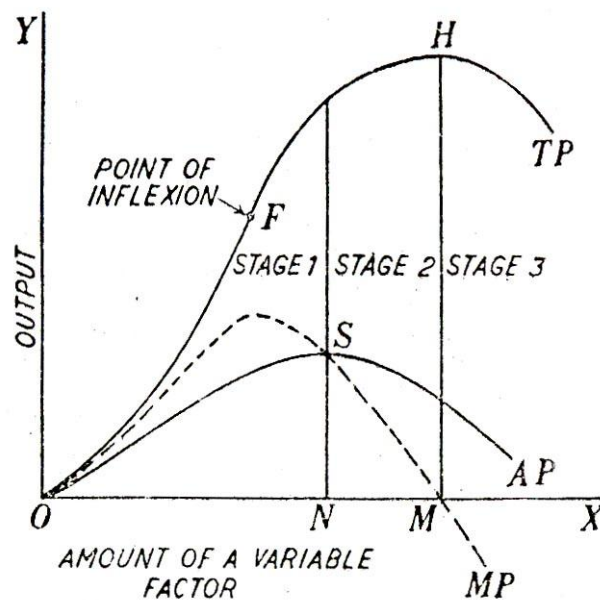


Fig. 4

Stage 1. In this stage, total product to a point increases at an increasing rate. In Fig. 4 from the origin to the point F, slope of the total product curve TP is increasing, that is, upto the point F, the total product increases at an increasing rate (the total product curve TP is concave upwards up to the point F), which means that the marginal product MP rises. From the point F onwards during the stage 1, the total product curve goes on rising but its slope is declining which means that from point F onwards the total product increases at a diminishing rate (total product curve is concave downwards), i.e., marginal product falls but is positive. The point where the total product stops increasing at an increasing rate and starts increasing at the diminishing rate is called the point of inflexion. Corresponding vertically to this point of inflexion marginal product is maximum, after which it slope downward.

The stage 1 ends where the average product curve reaches its highest point. During the stage 1, when marginal product of the variable factor is falling, it still exceeds its average product and so continues to cause the average product curve to rise. Thus, during the stage 1, whereas marginal product

curve rises in a part and then falls the average product curve rises throughout. In the first stage, the quantity of the fixed factor is too much relative to the quantity of the variable factor so that if some of the fixed factor is withdrawn, the total product would increase. Thus, in the first stage marginal product of the fixed factor is negative.

Stage 1 is known as the stage of increasing returns because average product of the variable factor increases throughout this stage. It is notable that the marginal product in this stage increases but in a later part it starts declining but remains greater than the average product so that the average product continues to rise.

Stage 2 : Stage of Diminishing returns. In stage 2, the total product continues to increase at a diminishing rate until it reaches its maximum point H where the second stage ends. In this stage both the marginal product and average product of the variable factor are diminishing but are positive. At the end of the second stage, that is, at point M marginal product of the variable factor is zero (corresponding to the highest point of the total product curve TP) Stage 2 is very crucial and important because the firm will seek to produce in its range. This stage is known as the stage of diminishing returns as both the average and marginal products of the variable factor continuously fall during this stage.

Stage 3 : Stage of Negative Returns. In stage 3 total product declines and therefore the total product curve TP slopes downward. As a result, marginal product of the variable factor is negative and the marginal product curve MP goes below the X-axis. In this stage, variable factor is too much relative to the fixed factor. This stage is called the stage of negative returns, since the marginal product of the variable factor is negative during this stage.

It may be noted that stage 1 and stage 3 are completely symmetrical. In stage 1 the fixed factor is too much relative to the variable factor. Therefore, in stage 1, marginal product of the fixed factor is negative. On the other hand, in stage 3 variable factor is too much relative to the fixed factor. Therefore, in stage 3, the marginal product of the variable factor is negative.

The Stage of Operation. Now an important question is in which stage a rational producer will seek to produce. A rational producer will never choose to produce in stage 3 where marginal product of the variable factor is negative. Marginal product of the variable factor being negative in stage 3, a producer can always increase his output by reducing the amount of variable factor. It is thus clear that a rational producer will never be producing in stage 3. Even if the variable factor is free, the rational producer stops at the end of the second stage where the marginal product of the variable factor is zero. At the end point M of the second stage where the marginal product of the variable factor is zero, the producer will be maximizing the total product and will thus be making maximum use of the variable factor.

A rational producer will also not choose to produce in stage 1 where the marginal product of the fixed factor is negative. A producer producing in stage 1 means that he will not be making the best use of the fixed factor and further he will not be utilizing fully the opportunities of increasing production by increasing quantity of the variable factor whose average product continues to rise throughout the stage 1. Thus a rational entrepreneur will not stop in stage 1 but will expand further. Even if the fixed factor is free (i.e., costs nothing), the rational entrepreneur will stop only at the end of stage 1 (i.e., at point N) where the marginal product of the fixed factor is zero and the average product of the variable factor is maximum. At the end point N of stage 1 he will be making maximum use of fixed factor.

It is thus clear from above that the rational producer will never be found producing in stage 1 and stage 3. Stage 1 and stage 3 may, therefore, be called stages of economic absurdity or economic nonsense. Thus stages 1 and 3 represent non-economic region in production function. A rational producer will always seek to produce in stage 2 where both the marginal product and average product of the variable factor are diminishing. At which particular point in this stage, the producer will decide to produce depends upon the prices of factors. The stage 2 represents the range of rational production decisions.

We have seen how the output varies as the factor proportions are altered at any given moment. We have also noticed that this input-output relation can be divided into three stages—stage 1 of increasing returns, stage 2 of diminishing returns, and stage 3 of negative returns.

Law of Variable Proportions Illustrated with the Help of Equal Product Curves

It will be instructive as well as interesting to show the operation of the law of variable proportions through equal product curves. Consider Fig. 5 in which a family of equal product curves has been drawn between the two factors X and Y measured on X-axis and F-axis respectively. It will be seen in Figure. HMX, that every equal product curve has a positive sloping portion on either end. Positive sloping portion of equal product curve implies that the marginal product of either factor becomes negative beyond a point. If factor X in the factor combination is increased (that is, if we move towards the right on any equal product curve), beyond a point its marginal. Three Stage, of the Law of Variable Proportion, marginal product becomes negative and therefore the equal product curve slopes upward beyond that point (upward or positive portion of the equal product curve means" that in the face of negative marginal product of a factor we have to increase the quantity of the other

factor whose marginal product is positive to keep output constant). Similarly, if the factor Y is increased on an equal product curve, beyond a point its marginal product becomes negative and therefore the equal product curve starts sloping upward. The lines OR and OQ separate the upward sloping portions of equal product curves from the other regions. Between the two lines OR and OQ all equal product curves are negatively sloping. The lines OR and OQ are called ridge lines.

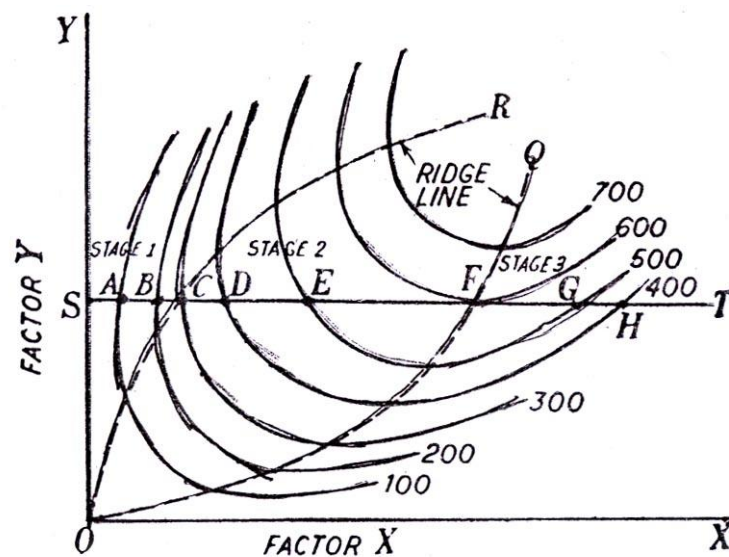


Fig. 5

Returns to Scale

CHANGES IN SCALE AND FACTOR PROPORTIONS

Factor proportions are altered by keeping the quantity of one or some factors fixed and varying the quantity of the other. The changes in output as a result of the variation in factor proportions, as seen before, forms the subject-matter of the “law of variable proportions.” We shall now undertake the study of changes in output when all factors or inputs in a particular production function are increased together. In other words, we shall now study the behaviour of output in response to the changes in the scale. An increase in the scale means that all inputs or factors are increased in the same proportion. Increase in the scale thus occurs when all factors or inputs are increased keeping factor proportions unaltered. The study of changes in output as a consequence of changes in the scale forms the subject-matter of ‘returns to scale’.

Before explaining returns to scale it will be instructive to make clear distinction between changes in the scale and changes in factor proportions. The difference between the changes in scale and changes in factor proportions will become clear from the study of Fig. 6 where two factors, labour and capital, have been measured on X-axis and Y-axis respectively. We suppose that only labour and capital are required to produce a particular product. An equal product map has been drawn. A point S has been taken on the Y-axis and the horizontal line ST parallel to X-axis has been drawn. OS represents the amount of capital which remains fixed along the line ST. As we move towards right on the line ST, the amount of labour varies while the amount of capital remains fixed at OS. In other words, proportion between the two factors undergoes a change along the line ST; the ratio of the variable factor ‘labour’ to the fixed factor ‘capital’ rises as we move to the right on the line ST. Thus the movement along the line ST represents variation in factor proportions. Likewise, a vertical line GH parallel to the Y-axis is drawn which

will also indicate changes in factor proportions. But in this case the quantity of labour will remain fixed while the quantity of capital will vary.

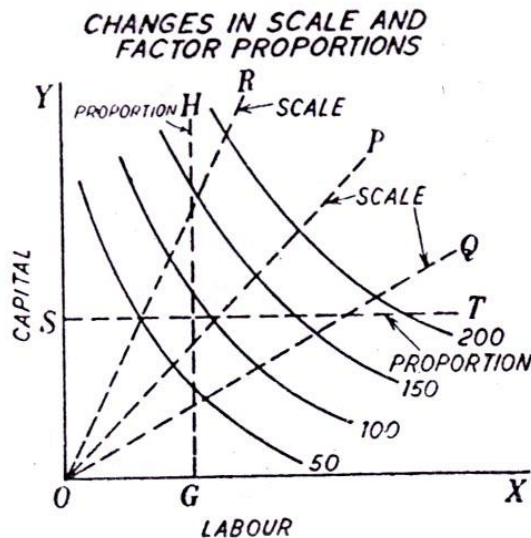


Fig. 6

Now, draw a straight line OP passing through the origin. It will be seen that along the line OP the inputs of both the factors, labour and capital, vary. Moreover, because the line OP is a straight line through the origin, the ratio between the two factors along OP will remain the same throughout. Thus, the upward movement along the line OP indicates the increase in the absolute amounts of two factors employed with the proportion between two factors remaining unchanged. Assuming that only labour and capital are needed to produce a product, then the increase in the two factors along the line OP represents the increase in the scale since along the line OP both the factors increase in the same proportion and therefore proportion between the two factors remains unaltered. If any other straight line through the origin such as OQ or OR is drawn, it will show, like the line OP, the changes in the scale but it will represent a different given proportion of factors which remains the same along the line. That is, the various straight lines through the origin will indicate different proportions between the two factors but on each line the proportion between the two factors will remain the same throughout.

Validity of the Concept of Returns to Scale

We now proceed to discuss how the returns vary with the changes in scale, that is, when all factors are increased in the same proportion. But some economists have challenged the concept of returns to scale on the ground that all factors cannot be increased and therefore the proportions between factors cannot be kept constant. For instance, it has been pointed out that entrepreneurship is a factor of production which cannot be varied (in the single firm), though all other factors can be increased. The entrepreneur and his decision-making are indivisible and incapable of being increased. Thus the entrepreneur is a fixed factor in all production functions. If labour and capital could produce a product with no one to supervise and take decisions, then the returns to scale in the sense of returns to all factors could be visualized. But the idea that labour and capital can produce goods without an entrepreneur is quite unrealistic. Thus, the concept of returns to scale involves a puzzle for economists which still remains unsolved. However, this puzzle can be solved by assuming entrepreneurship to be variable in the sense that the greater the other inputs or factors, the greater the entrepreneurial work to be performed.

But we shall explain below the concept of returns to scale by assuming that only two factors labour and capital are needed for production.

CONSTANT RETURNS TO SCALE

Returns to scale may be constant, increasing or decreasing. If we increase all factors (i.e., scale) in a given proportion and the output increases in the same proportion, returns to scale are said to be constant. Thus, if a doubling or trebling of all factors causes a doubling or trebling of outputs, returns to scale are constant. SB, if the increase in all factors leads to a more than proportionate increase in output, returns to scale are said to be increasing. Thus, if all factors are doubled and output increases by more than a double,

then the returns to scale are increasing. On the other hand, if the increase in all factors leads to a less than proportionate increase in output, returns to scale are decreasing. We shall explain below these various types of returns to scale.

As said above, the constant returns to scale means that with the increase in the scale or the amounts of all factors leads to a proportionate increase in output, that is, doubling of all inputs doubles the output. In mathematics the case of constant returns to scale is called linear and homogeneous production function or homogeneous production function of the first degree. Production function exhibiting constant returns to scale possesses very convenient mathematical properties which make it very useful for theoretical analysis. There are a number of special theorems which apply when production function exhibits constant returns to scale. Empirical evidence suggests that production function for the economy as a whole is not too far from being homogeneous of the first degree. Empirical evidence also suggests that in the production function for an individual firm there is a long phase of constant returns to scale.

Let us illustrate diagrammatically the constant returns to scale with the help of equal product curves. Fig. 7 depicts an equal product map. It is assumed that, in the production of the good, only two factors, labour and capital, are used. In order to judge whether or not returns to scale are constant, we draw some straight lines through the origin. As shown above, these straight lines passing through the origin indicate the increase in scale as we move upward. It will be seen from the figure that successive equal product curves are equidistant from each other along each straight line drawn from the origin.

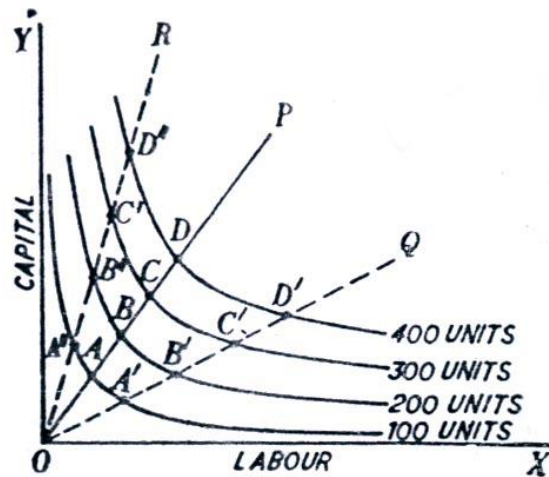


Fig. 7

Thus along the line OP, $AB=BC=CD$, and along the line OQ, $A'B'=B'C' = C'D'$ and along the line OR, $A'B'=B''G''=G''D'$. The distance between the successive equal product curves being the same along any straight line through the origin, means that if both labour and capital are increased in a given proportion, output expands by the same proportion.

MODULE – 2 TIME VALUE OF MONEY

The value/ purchasing power of a money at a particular time is called time value of money. A rupee today is worth more than a rupee will be received tomorrow. The present money income expected at a future date is lower than the money held today.

Money has time value. Money today is valued more because.

- (i) Money gives liquidity, and an opportunity to invest it and earn return (interest) on it.
- (ii) Individuals, in general prefer current consumption to future consumption because the future is always uncertain and involves risk.
- (iii) Capital can be employed productively to generate positive returns.
- (iv) In an inflationary period a rupee represents real purchasing power than a rupee a year hence.

Since money has earning as well as purchasing power, money has time value.

For example, suppose you have deposited Rs. 200/- in a bank with 10% rate of interest. After one year the interest would be 20 and the amount will become Rs. 220/- at the end of the year. It follows that Rs. 220/- expected one year hence is worth only Rs. 200/- today.

TECHNIQUES FOR ADJUSTING TIME VALUE OF MONEY OR INTEREST FORMULAS

While making investment decisions, computations will be done in many ways. To simplify all these computations, it is extremely important to know how to use interest formulas more effectively. Before discussing the effective application of the interest formulas for investment-decision making, the various interest formulas are presented.

Interest rate can be classified into simple interest rate, and compound interest rate. In simple interest, the interest is calculated, based on the initial deposit for every interest period. In compound interest, the interest for the current period is computed based on the amount (principal plus interest up to the end of the previous period) at the beginning of the current period.

The notations which are used in various interest formulae are as follows:

P = principal amount

n - No. of interest periods

i = interest rate (It may be compounded monthly, quarterly, semiannually or annually)

F - future amount at the end of year n

A = equal amount deposited at the end of every interest period

G = uniform amount which will be added/subtracted period after period to/from the amount of deposit A at the end of period 1

1. Single-Payment Compound Amount / Future value of an amount

Here, the objective is to find the single future-sum (F) of the initial payment (P) made at time 0 after n periods at an interest rate i compounded every period.



Fig. 1 : Cash flow diagram of single-payment compound amount.

The formula to obtain the single-payment compound amount is

$$F = P(1+i)^n$$

$$\text{Or } F = P(F/P, i, n)$$

where

$(F/P, i, n)$ is called as single-payment compound amount factor.

EXAMPLE I : A person deposits a sum of Rs. 20,000 at the interest rate 18% compounded annually for 10 years. Find the maturity value after 10 year.

Solution

$P = \text{Rs. } 20,000$

$i = 18\%$ compounded annually

$n = 10$ years $F = P(1+i)^n = P(F/P, i, n)$

$= 20,000 (F/P, 18\%, 10)$

$= 20,000 \times 5.234 = \text{Rs. } 1,04,680$

The maturity value of Rs. 20,000 invested now at 18% compounded yearly is equal to Rs.1,04,680 after 10 years.

2. Single Payment present worth amount

Here, the objective is to find the present worth amount (P) of a single future (F) which will be received after n periods at an interest rate of compound at the end of every interest period.

The corresponding cash flow diagram is shown in Fig. 2

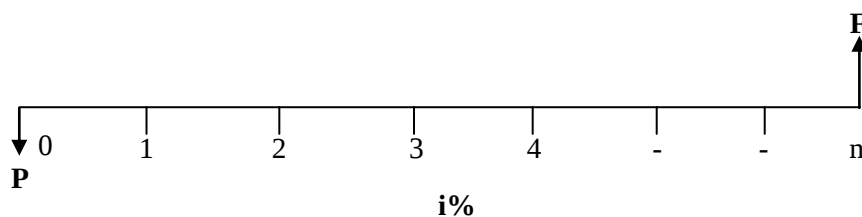


Fig 2. Cash flow diagram of single-payment present worth amount.

The formula to obtain the present worth is

$$P = \frac{F}{(1+i)^n} = F(P/F, i, n)$$

Example 2

A person wishes to have a future sum of Rs. 1,00,000 for his son's education after 10 years from now. What is the single-payment that the deposit now so that he gets the desired amount after 10 years? The bank gives 15% interest rate compounded annually.

Solution

F = Rs.1,00,000

i = 15%, compounded annually

n = 10 years

$p = F / (1+i)^n = F(P/F, i, n)$

= 1,00,000 (P/F, 15%, 10)

= 1,00,000 x 0.2472

= Rs. 24,720

The person has to invest Rs.24,720 now so that he will get a sum of Rs.1,00,000 after 10 years at 15% interest rate compounded annually.

3. Equal-Payment Series Compound Amount / Future value of an annuity

The objective is to find the future worth of n equal payments which are made at the end of every interest period till the end of the nth interest period at an interest rate of compounded at the end of each period. The corresponding cash flow diagram is shown in Fig. 3.

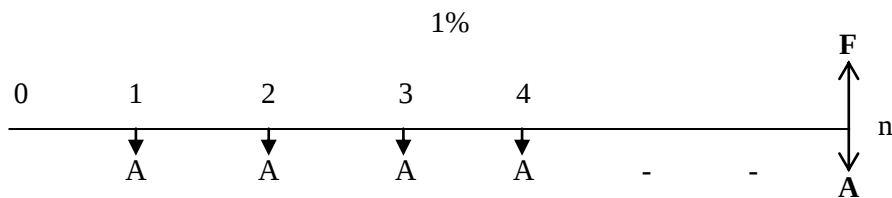


Fig. 3 : Cash flow diagram of equal-payment series compound amount.

Equal amount deposited at the end of each interest period = A

No. of interest periods = n

Rate of interest = i

Single future amount = F

The formula to get F is

$$F = A \left[\frac{(1+i)^n - 1}{i} \right] = A(F/A, i, n)$$

Where (F/A, i, n) is termed as equal-payment series compound amount factor.

Example 3 : A person who is not 35 years old is planning for his retired life. He plans to invest an equal sum of Rs.10,000 at the end of every year for the next 25 years starting from the end of the next year. The bank gives 20% interest rate, compounded annually. Find the maturity value of his account when he is 60 years old.

Solution

A = Rs. 10,000

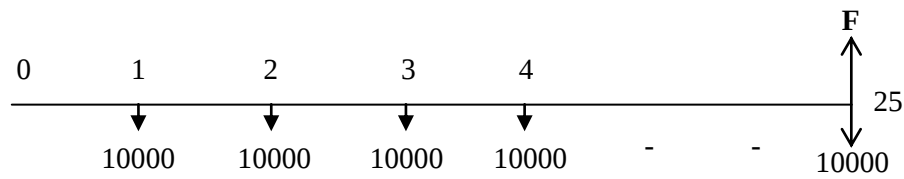
n = 25 years

i = 20%

F = ?

The corresponding cash flow diagram is shown below :

$$i = 20\%$$



Cash flow diagram of equal-payment series compound amount.

$$F = A \frac{(1+i)^n - 1}{i}$$

$$= A (F/A, i, n)$$

$$= 10,000 (F/A, 20\%, 25)$$

$$= 10,000 \times 471.981$$

= Rs. 47,19,810 The future sum of the annual equal payments after 25 years is equal to Rs. 47,19,810.

4. Equal-Payment Series Sinking Fund

In this type of investment mode, the objective is to find the equivalent amount (A) that should be deposited at the end of every interest period for n interest periods to realize a future sum (F) at the end of the nth interest period at an interest rate of i

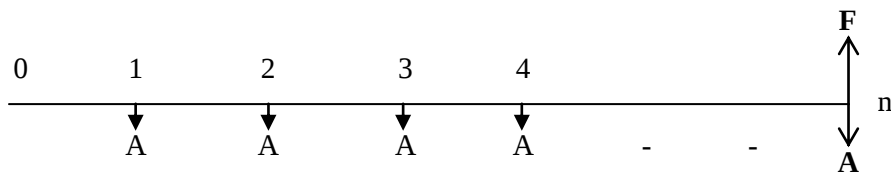


Fig. 4.: Cash flow diagram of equal payment series sinking fund

A = equal amount to be deposited at the end of each interest period

n = No. of interest periods / i = rate of interest

F = single future amount at the end of the nth period

The formula to get F is

$$A = F \frac{i}{(1+i)^n - 1} = F(A/F, i, n)$$

where

(A/F, i, n) is called as equal-payment series sinking fund factor.

EXAMPLE

A company has to replace a present facility after 15 years at an outlay of Rs.5,00,000. It plans to deposit an equal amount at the end of every year for the next 15 years at an interest rate of 18% compounded annually. Find the equivalent amount that must be deposited at the end of every year for the next 15 years.

Solution

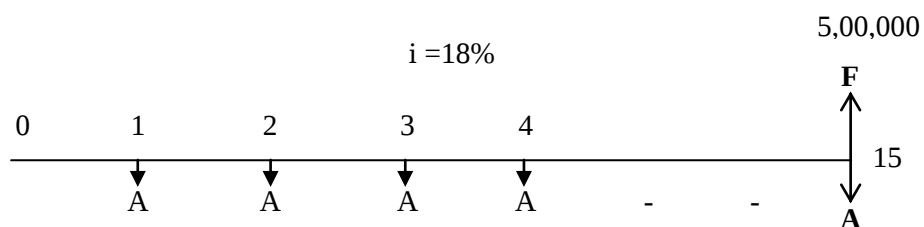
F = Rs. 5,00,000

n = 15 years

i = 18%

A = ?

The corresponding cash flow diagram is shown below



Cash flow diagram of equal-payment series sinking fund.

$$A = F \frac{i}{(1+i)^n - 1} = F(A/F, i, n)$$

$$= 5,00,000 (A/F, 18\%, 15)$$

$$= 5,00,000 \times 0.0164$$

$$= \text{Rs.} 8,200$$

The annual equal amount which must be deposited for 15 years is Rs.8,200.

5. Equal Payment Series Present worth amount

The objective of this mode of investment is to find the present worth of an equal payment made at the end of every interest period for n interest periods at interest rate of i compounded at the end of every interest period.

The corresponding cash flow diagram is shown in Fig. 5. Here,

P - present worth

A = annual equivalent payment

i = interest rate

n = No. of interest periods

The formula to compute P is

$$P = A \frac{(1+i)^n - 1}{i(1+i)^n} = A(P/A, i, n)$$

where $(P/A, i, n)$ is called equal-payment series present worth factor.

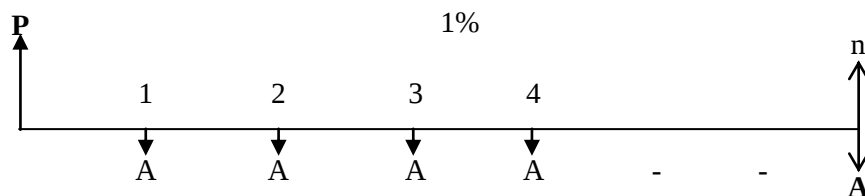


Fig. 5 : Cash flow diagram of equal-payment series present worth amount.

EXAMPLE 5 : A company wants to set up a reserve which will help company to have an annual equivalent amount of Rs. 10,00,000 for the next years towards its employees welfare measures. The reserve is assumed to grow the rate of 15% annually. Find the single-payment that must be made now the reserve amount.

Solution

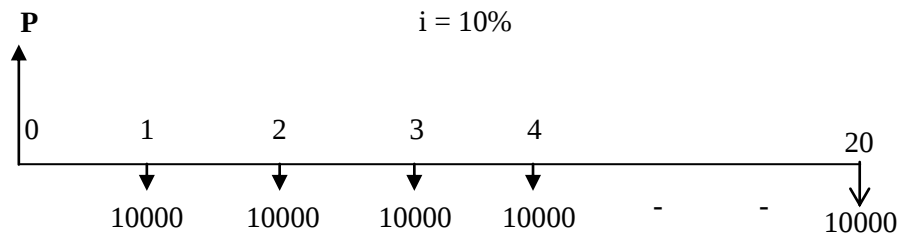
$$A = \text{Rs.}10,00,000$$

$$i = 15\%$$

$$n = 20 \text{ years}$$

$$P = ?$$

The corresponding cash flow diagram is illustrated below :



Cash flow diagram of equal-payment series present worth amount.

$$P = A \frac{(1-i)^n - 1}{i(1+i)^n} = A(P/A, i, n)$$

$$= 10,00,000 \times (P/A, 15\%, 20)$$

$$= 10,00,000 \times 6.2593$$

$$= \text{Rs.}62,59,300$$

The amount of reserve which must be set-up now is equal to Rs.62,59,300.

6. Equal-Payment Series Capital Recovery Amount

The objective of this mode of investment is to find the annual equivalent amount (A) which is to be recovered at the end of every interest period for n interest periods for a loan (P) which is sanctioned now at an interest rate of i compounded at the end of every interest period.

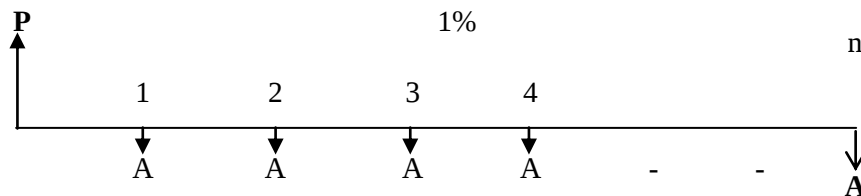


Fig. 6 : Cash flow diagram of equal-payment series capital recovery amount.

P - present worth (loan amount)

A = annual equivalent payment (recovery amount)

i = interest rate

n - No. of interest periods

The formula to compute P is as follows:

$$A = P \frac{i(1+i)^n}{(1+i)^n - 1} = P(A/P, i, n)$$

where,

(A/P, i, n) is called equal-payment series capital recovery factor.

EXAMPLE 6 A bank gives a loan to a company to purchase an equipment worth Rs. 10,00,000 at an interest rate of 18% compounded annually. This amount should be repaid in 15 yearly equal installments. Find the installment amount that the company has to pay to the bank.

Solution

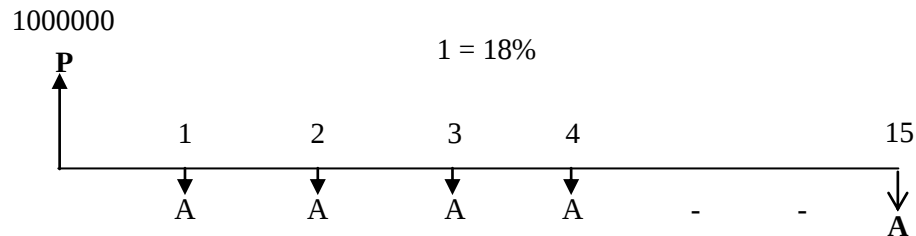
$P = \text{Rs. } 10,00,000$

$i = 18\%$

$n = 15 \text{ years}$

$A = ?$

The corresponding cash flow diagram is shown below:



Cash flow diagram of equal-payment series capital recovery amount.

$$A = P \frac{i(1+i)^n}{(1+i)^n - 1} = P(A/P, i, n)$$

A) Present Worth Method

In all engineering problems the engineers encounter one important question, i.e., which project to select. To select among the different alternatives different methods have been evolved. There are several bases for comparing the worthiness of the projects. These bases are

1. Present worth method
2. Future worth method
3. Annual equivalent method
4. Rate of return method

5. Pay back period

Present worth method is one of them. Many economists prefer a present worth analysis because it reveals the sum in today's rupee that is equivalent to a future cash flow stream. For example – Rs.110/- expected one year hence is worth only Rs.100/- today, if the rate of interest is 10%, compounded annually. This means that Rs.100/- is the present value of Rs.110/- to be earned one year hence.

Under this method, the present worth of all cash inflows (revenues) is compared against the present worth of all cash outflows (costs) associated with an investment project. In this method of comparison, the cash flow of each alternative will be reduced to time zero by assuming an interest rate i . Then, depending on the type of decision, the best alternative will be selected by comparing the present worth amounts of the alternatives. The difference between the present worth of the cash flows (inflows – outflows) referred to as the Net Present Worth. NPW determines whether or not the project is an acceptable investment.

Conditions for Present worth Comparison

- (i) Estimate the interest rate that the firm wishes to earn on its investment.
- (ii) Determine the service life of the project.
- (iii) Determine the cash inflows over each service life.
- (iv) Determine the cash overflows over each service period.
- (v) Estimate the net cash flows (inflows – outflows).

If there is single investment proposal, whether a project will be selected or rejected that can be made accordingly.

If $PW > 0$, select the proposal. A positive NPW means the equivalent worth of the inflows is greater than the equivalent worth of outflows. So, the project makes profit.

If $PW < 0$, reject the investment project. A negative NPW means the equivalent worth of the inflows is less than the equivalent worth of outflows.

If $PW = 0$, remain indifferent to the investment.

If we have mutually exclusive alternatives then present worth cash flows can be calculated by two prominent methods. These are

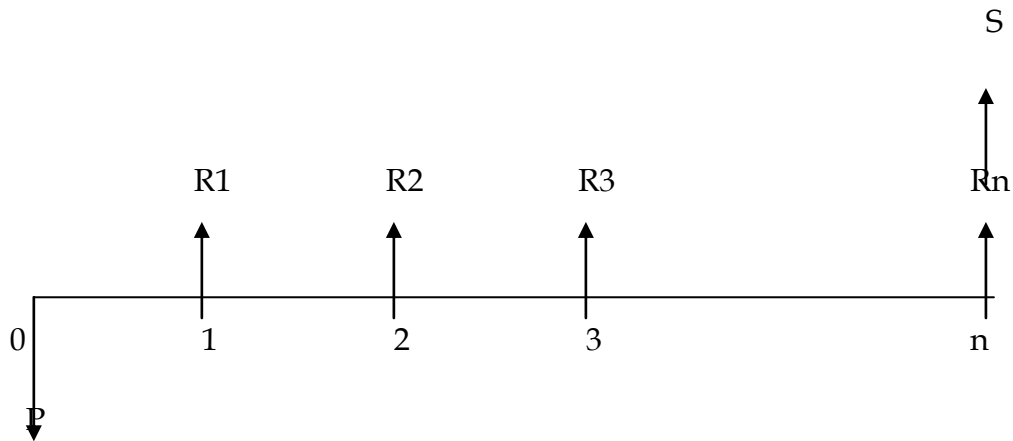
- (i) Revenue based present worth
- (ii) Cost based present worth.

In a revenue/ profit dominated cash flow diagram, the profit, revenue, salvage value (all inflows to an organization) will be assigned with positive sign. The costs (out flows) will be assigned with negative sign.

In a cost dominated cash flow diagram the costs (out flows) will be assigned with positive sign and the profit, revenue, salvage value (all inflows) etc. will be assigned with negative sign. In case the decision is to select the alternative with the maximum profit, then the alternative with the maximum present worth will be selected.

If the decision is to select the alternative with the minimum cost, then the alternative with the least present worth amount will be selected.

Revenue dominated cash flow diagram



Where 'P' is the initial investment

'Rn' is the net revenue at the end of nth year.

'i' is the interest rate compounded annually

'S' is the salvage value at the end of the nth year.

To find the present worth of the cash flow from the above diagram for a given interest rate, the formula is

$$PW(i) = -P + \frac{R_1}{(1+i)^1} + \frac{R_2}{(1+i)^2} + \dots + \frac{R_n}{(1+i)^n} + \frac{S}{(1+i)^n}$$

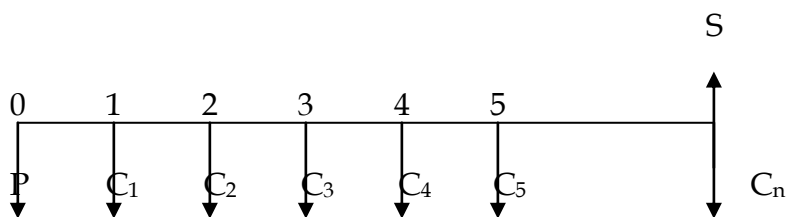
Or

$$PW(i) = -P + R_1(P/F, i, 1) + R_2(P/F, i, 2) + \dots + R_n(P/F, i, n) + S(P/F, i, n)$$

If it is a uniform series or equal payment series then the formula will be

$$PW(i) = -P + R(P/F, i, n) + S(P/F, i, n)$$

Cost dominated cash flow diagram



Where 'P' is the initial investment

'C_n' is the net cost of operation and maintenance at the end of the nth year

'S' is the salvage value at the end of the nth year

'C_i' is the discounted rate of interest

and for it the present worth expression is

$$PW(i) = P + \frac{C_1}{(1+i)^1} + \frac{C_2}{(1+i)^2} + \dots + \frac{C_n}{(1+i)^n} - \frac{S}{(1+i)^n}$$

Or

$$PW(i) = -P + C_1(P/F, i, 1) + C_2(P/F, i, 2) + \dots + C_n(P/F, i, n) - S(P/F, i, n)$$

It is a uniform series or equal payment series then the formula will be

$$PW(i) = P + C(P/F, i, n) - S(P/F, i, n)$$

Examples

In this section, the concept of present worth method of comparison applied to the selection of the best alternative is demonstrated with several illustrations.

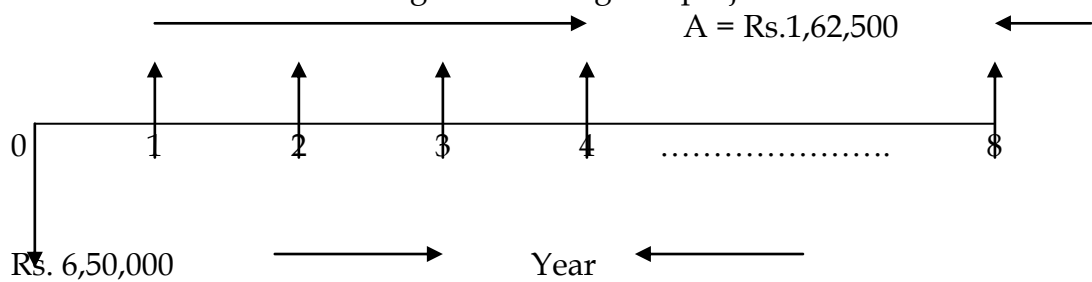
Example 1 : the following table summarizes a cash flow stream of an investment project.

Year (n)	Net cash flows (Rs.)
0	-6,50,000
1	1,62,500
2	1,62,500
3	1,62,500
4	

5	
6	
7	
8	1,62,500

If the firm's rate of interest is 15%, compute the NPW of this project. Is this project acceptable ?

Solution : The cash flow diagram for the given project is



This is a uniform cash flow stream. Since the project requires an initial investment of Rs. 6,50,000 at present ($n = 0$) followed by 8 equal annual receipt of Rs. 1,62,500, we can easily determine the NPW as follows :

$$\begin{aligned}
 \text{NPW} &= -P + R (P/A, i, n) \\
 &= - \text{Rs. } 6,50,000 + \text{Rs. } 1,62,500 (P/A, 15\%, 8) \\
 &= - \text{Rs. } 6,50,000 + \text{Rs. } 1,62,500 (4.4873) \\
 &= - \text{Rs. } 6,50,000 + \text{Rs. } 7,92,190 \\
 &= \text{Rs. } 79,190
 \end{aligned}$$

Since, $\text{PW } (15\%) > 0$, the project would be acceptable.

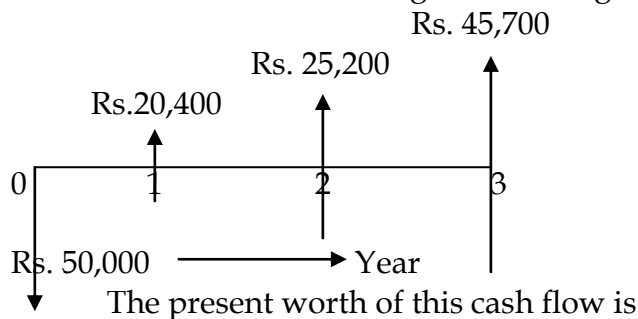
Example 2 : The project cash flows of an investment proposal is given below.

End of Year	Net cash flows (Rs.)
0	-50,000
1	20,400

2	25,200
3	45,750

Evaluate the economic desirability of this project for $i = 10\%$.

Solution : The cash flow diagram for the given project is shown below :



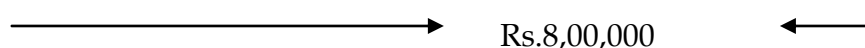
$$\begin{aligned}
 PW(10\%) &= -50,000 + 20,400 (P/F, 10\%, 1) + 25,200 (P/F, 10\%, 2) + 45,750 (P/F, 10\%, 3) \\
 &= -50,000 + 20,400 (0.9091) + 25,200 (0.8264) + 45,750 (0.7513) \\
 &= \text{Rs. } 23742.89
 \end{aligned}$$

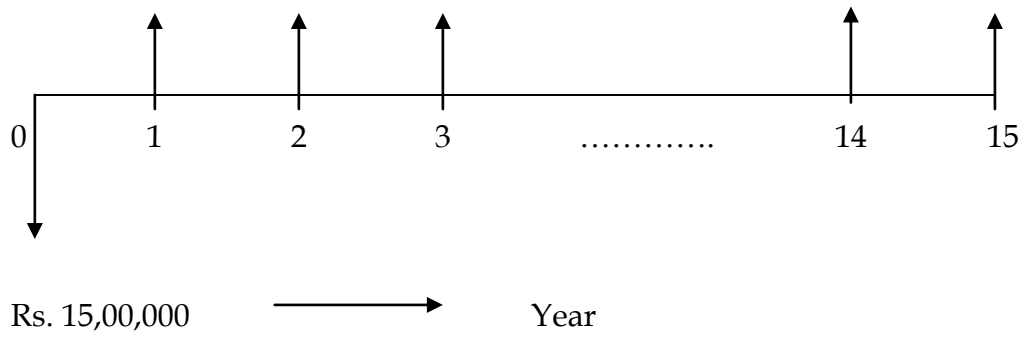
Since $PW(10\%) > 0$, the project is acceptable.

Example 3 : Given the following information, suggest the best alternative which is to be implemented based on the present worth method, assuming 20% interest rate compounded annually.

Alternative	Initial Cost	Annual Revenue	Life
A	Rs.15,00,000	Rs. 8,00,000	15 years
B	Rs. 20,00,000	Rs. 6,00,000	15 years
C	Rs. 16,00,000	Rs. 4,00,000	15 years

Solution : The cash flow diagram for alternative A is

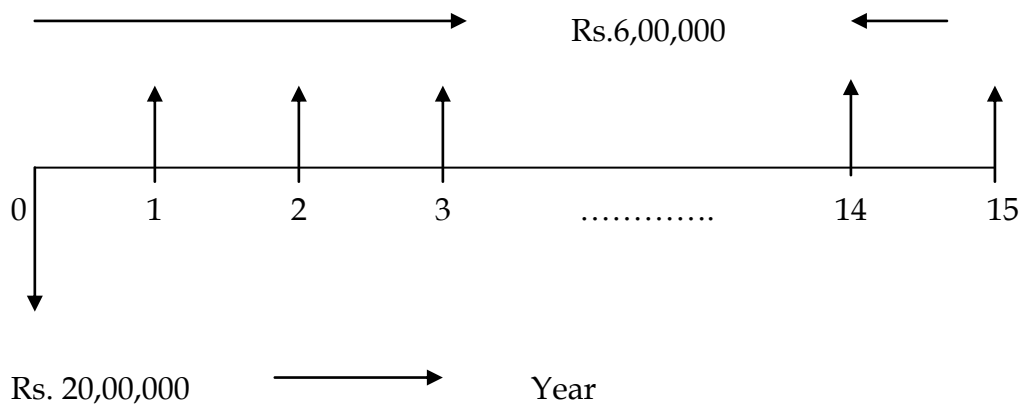




The present worth for this cash flow is

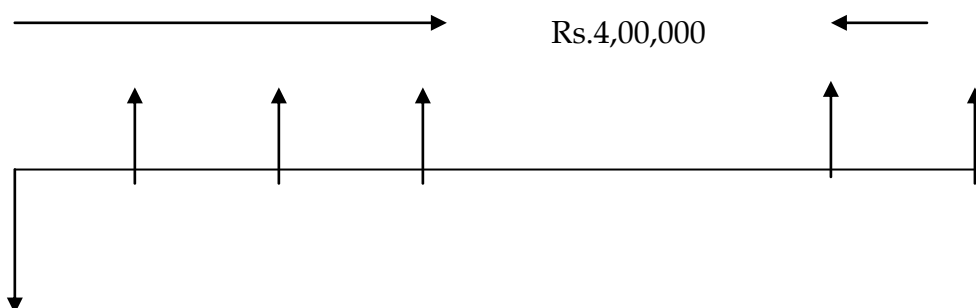
$$\begin{aligned}
 PW(20\%)_A &= - \text{Rs. } 15,00,000 + \text{Rs. } 8,00,000 (P/A, 20\%, 15) \\
 &= - \text{Rs. } 15,00,000 + \text{Rs. } 8,00,000 (4.6755) \\
 &= \text{Rs. } 22,40,400
 \end{aligned}$$

The cash flow diagram for alternative B is



$$\begin{aligned}
 PW(20\%)_B &= - \text{Rs. } 20,00,000 + \text{Rs. } 6,00,000 (P/A, 20\%, 15) \\
 &= - \text{Rs. } 20,00,000 + \text{Rs. } 6,00,000 (4.6755) \\
 &= \text{Rs. } 8,05,300
 \end{aligned}$$

The cash flow diagram of alternative C is



0 1 2 3 14 15

Rs. 16,00,000 $\longrightarrow$ Year

$$PW(20\%)_C = - \text{Rs. } 16,00,000 + \text{Rs. } 4,00,000 (P/A, 20\%, 15)$$

$$= - \text{Rs. } 16,00,000 + \text{Rs. } 4,00,000 (4.6755)$$

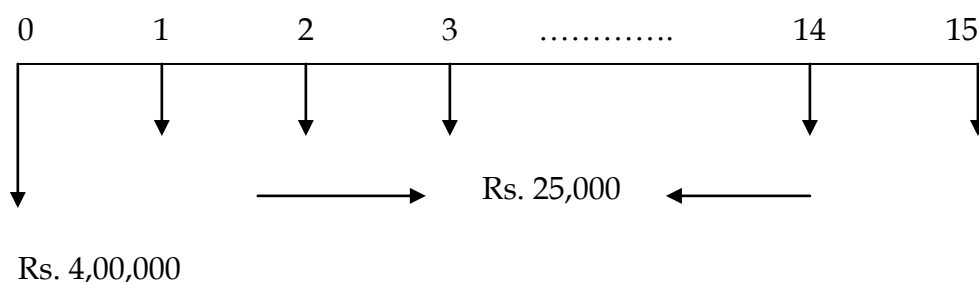
$$= \text{Rs. } 2,70,200$$

Since the present worth of alternative A is the highest among all the alternatives so it is suggested for implementation.

Example 4 : Given the following information, suggest which technology should be selected based on present worth method, assuming 15% interest rate compounded annually.

Technology	Initial Cost (Rs.)	Service Life	Annual O & M Cost
A	4,00,000	15 Years	25,000
B	5,00,000	15 Years	29,000

Solution : The cash flow diagram of technology A is



The present worth amount of this cash flow stream is

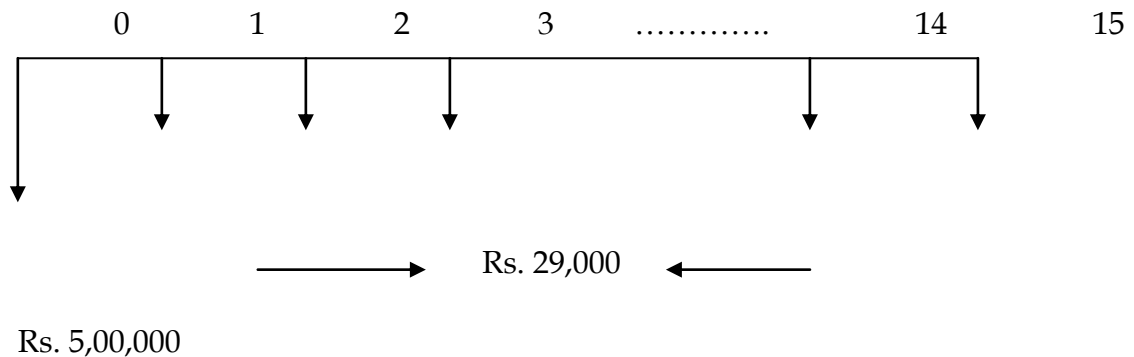
$$PW(15\%)_A = \text{Rs. } 4,00,000 + \text{Rs. } 25,000 (P/A, 15\%, 15)$$

$$= \text{Rs. } 4,00,000 + \text{Rs. } 25,000 (5.8474)$$

$$= \text{Rs. } 4,00,000 + \text{Rs. } 1,46,185$$

$$= \text{Rs. } 5,46,185$$

The cash flow diagram for technology B is



$$PW(15\%)_B = \text{Rs. } 5,00,000 + \text{Rs. } 29,000 (P/A, 15\%, 15)$$

$$= \text{Rs. } 5,00,000 + \text{Rs. } 29,000 (5.8474)$$

$$= \text{Rs. } 5,00,000 + \text{Rs. } 1,69,574.6$$

$$= \text{Rs. } 6,69,574.6$$

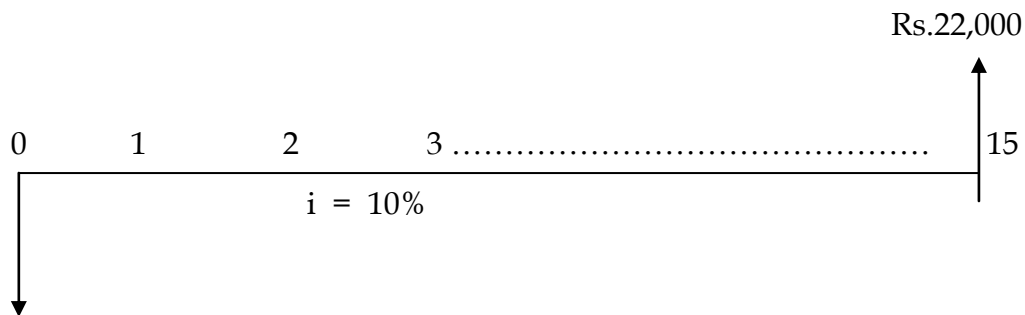
Since PW amount of technology A is lower, hence technology A is to be selected.

Example 5 : A finance company advertises two investment plans. In plan 1 the company pays Rs. 22,000 after 15 years for every Rs.1,000 invested now. In plan 2, for every Rs. 1,000 invested the company pays Rs. 4,000 at the end of the 10th year and Rs. 4,000 at the end of 15th year. Select the best investment plan at $i = 10\%$ compounded annually.

Solution :

Plan 1 : Cash flow diagram for plan 1 is

The cash flow diagram of alternative C is



B) FUTURE WORTH METHOD

Future worth method is particularly useful in an investment situation where we need to compute the equivalent worth of a project at the end of its investment period rather than at its beginning.

Conditions for computing Future Worth Method

1. Determine the interest rate
2. Estimate the service life of the project
3. Estimate the cash inflows for each period over the service life.
4. Estimate the cash outflows over each service period.
5. Determine the net cash flows (inflows – outflows).

For a single project evaluation

If $FW > 0$, project is accepted.

If $FW < 0$, reject the investment proposal.

If $FW = 0$, remain indifferent to the investment.

For a mutually exclusive alternatives future worth cash flows can be calculated by

- i) Revenue based future worth
- ii) Cost based future worth.

In revenue based cases the alternative with maximum future worth amount will be selected. In cost based cases the alternative with the least future worth amount will be accepted.

The formula for the future worth for a given interest rate i is

$$FW(i) = -P(1+i)^n + R_1(1+i)^{n-1} + R_2(1+i)^{n-2} + \dots + R_n + S$$

Or

$$FW(i) = -P(F/P, i, n) + R_1(F/P, i, n-1) + R_2(F/P, i, n-2) + \dots + R_n + S$$

If it is equal payment series then the formula will be

$$FW(i) = -P(F/P, i, n) + R(F/P, i, n) + S$$

In these cases the alternative with the maximum future worth amount should be selected as the best alternative.

If the cash flow stream is cost-based, then the future worth is given by

$$FW(i) = P(1+i)^n + C_1(1+i)^{n-1} + C_2(1+i)^{n-2} + \dots + C_n - S$$

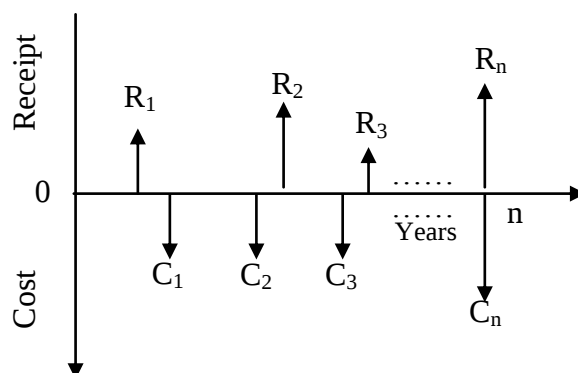
Or

(C) EQUIVALENT ANNUAL WORTH COMPARISON (EAW)

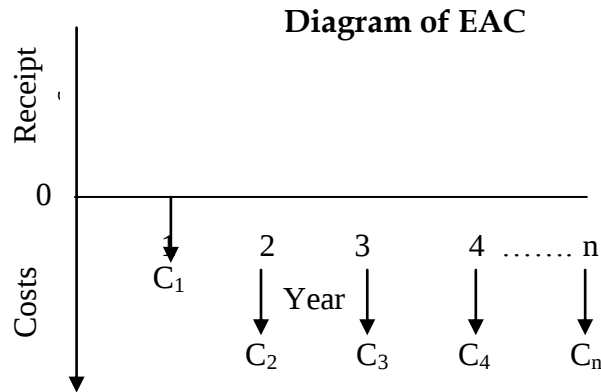
There are various alternatives for comparing the worthiness of a project. Equivalent Annual Worth (EAW) is one important method for comparing engineering alternatives. In an annual worth method, all the receipts and disbursements occurring over a period are converted to an equivalent uniform yearly amount. EAW is a popular method because of a year's profit and losses are taken into account. A large number of engineering economic decisions are based on annual comparison and so the term equivalent uniform yearly amount often used. For example, cost accounting procedures, depreciation charges, tax calculations etc. These yearly cost tabulations generally make the annual worth method easier.

Equivalent Annual Cost (EAC) indicates that the equivalent value of negative cash flow for disbursement is greater than the corresponding positive flow of receipts.

Diagram of EAW



We will use the term equivalent annual worth (EAW) when costs and receipts are both present.



We will use the term equivalent annual cost (EAC) to designate comparison involving only costs.

Conditions for Computing EAW

1. Estimate the cash flows (inflows, outflows) over each service period.
2. Estimate the service life of the project.
3. Determine the interest rate.
4. Comparisons are made with before-tax cash flows.
5. EAW comparisons do not include intangible considerations.

For single alternatives if

$EAW > 0$, Accept the investment proposal

$EAW < 0$, Reject the investment proposal

$EAW = 0$, Remain indifferent to the investment.

For multiple alternatives or mutually exclusive alternatives if all the alternatives are revenue dominated, the all the alternatives are revenue dominated, the alternative with higher EAW will be selected. If all the alternatives are cost based, the alternatives with least EAW will be accepted.

EAW consists of following steps

- i. complete the net present worth (NPW)

- ii. Multiply the amount of present worth by the capital recovery factor. i.e.
 $EAW = PW(i) (A/P, i, n)$ where $(A/P, i, n)$ is called equal-payment series capital recovery factor .

The annual equivalent worth can be computed by using the general formula.

$$\text{i.e., } EAW = PW(i) \frac{i(1+i)^n}{(1+i)^{n-1}}$$

Example 1

Consider a machine that costs Rs.40,000 and a 10 year useful life. At the end of 10 year, it can be sold for Rs.5,000 after tax adjustment. If the firm could earn an after-tax revenue of Rs.10,000 per year with this machine, should it be purchased at an interest rate of 15%, compounded annually.

Solution

Initial cost (P) – Rs.40,000/-

Useful life (n) – 10 years

Salvage value - Rs. 5,000/-

Revenue – Rs.10,000/-

$i = 15\%$, compound annually

The cash flow diagram for the given project is

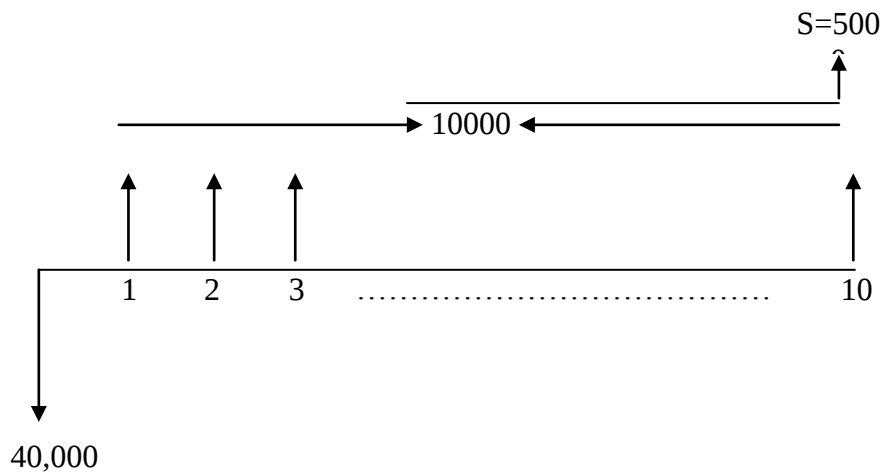


Fig. 1 : Cashflow diagram of this project

Step 1 - To find out NPW (15%)

$$PW (15\%) = -P + R(P/A, i, n) + S(P/F, i, n)$$

$$= -40,000 + 10,000 (P/A, 15\%, 10)$$

$$+ 5,000 (P/F, 15\%, 10)$$

$$= -40,000 + 10,000 (5.0188)$$

$$+ 5000 (0.2472)$$

$$= \text{Rs. } 11,424/-$$

Step II

$$EAW (15\%) = PW(i) (A/P, i, n)$$

$$= \text{Rs. } 11424 (A/p, 15\%, 10)$$

$$= \text{Rs. } 11424 (0.1993)$$

$$= \text{Rs. } 2276.80$$

Since $EAW (15\%) > 0$, so the project is accepted

There will be an equivalent profit of Rs.2276.8 per year over the machine life.

D. RATES OF RETURN METHOD

The rate of return is a percentage that indicates the relative yield on different uses of capital. Three rates of return appear frequently in engineering economy studies:

- The minimum acceptable rate of return (MARR) is the rate set by an organization to designate the lowest level of return that makes an investment acceptable.
- The internal rate of return (IRR) is the rate on the unrecovered balance of the investment in a situation where the terminal balance is zero. It is a discount rate at which $NPV = 0$.
- The external rate of return (ERR) is the rate of return that is possible to obtain for an investment under current economic conditions. For example, suppose that analysis of an investment shows that it will realize an IRR of 50 percent. Rationally, it is not reasonable to expect that we can invest in the external market and get that high a rate. In engineering economy studies, the external interest rate most often will be set to the MARR.

MINIMUM ACCEPTABLE RATE OF RETURN

The minimum acceptable rate of return, also known as the minimum attractive rate of return, is a lower limit for investment acceptability set by organizations or individuals. It is a device designed to make the best possible use of a limited resource, i.e., money. Rates vary widely according to the type of organization, and they vary even within the organization. Historically, government agencies and regulated public utilities have utilized lower required rates of return than have 'competitive industrial enterprises. Within a given enterprise, the required rate may be different for various divisions or activities. These variations usually reflect the risk involved. For instance, the rate of return required for cost reduction proposals may be lower than that required for research and development projects in which there is less certainty about prospective cash flows.

INTERNAL RATE OF RETURN

The IRR is the best-known and most widely used rate-of-return method. It is also known as the true rate-of-return method and the discounted cash flow method. The internal rate of return, represented by i in the traditional interpretation of interest rates, is the rate of interest earned by an alternative investment on the unrecovered balance of an investment.

The internal rate of return can be calculated by equating the annual, present, or future worth of cash flow to zero and solving for the interest rate (IRR) that allows the equality, it should be added that solving for the interest rate in this manner results in a polynomial equation that is a function of i , which may result in multiple roots of the equation (). In such cases the IRR may or may not be one of the equation roots.

Although both the EAW and FW approaches are legitimate, the rate of return is often defined in terms of present worth, under the constraints of possible i^* roots, where the IRR is

- The interest rate at which the present worth of the cash flow of a project is zero, or, to restate this in another way:
- The rate which when employed in computing the present worth of all costs and present worths of all returns will make them equal

Because rate-of-return computations usually begin with a problem expressed in terms of present worth or annual worth, it is necessary to pay attention to the guidelines for the EAW and PW methods. In particular, mutually exclusive alternatives (where selection of one precludes selection of others) must be compared on the basis of equivalent outcomes. In the case of independent alternatives (the choice of one does not affect the choice of another, except for limited capital availability), all costs and benefits must be explicitly stated.

Calculation of IRR

Determining the IRR is a function of the type of investment (simple, pure, and mixed) and the characteristics of the alternatives (mutually exclusive or independent). If we have independent projects, we may fund combinations of the projects since an independent project does not affect the funding of another project (except for capital availability limitations which are very real in most situations analyzed by the engineering economist). The cash flows of several independent alternatives that are being considered as a group may be summed to form the group's composite cash flow. Analysis can then be performed on this composite cash flow. Where capital limitations are apparent in a department and several independent alternatives are competing for funding, combinations of alternatives may be formed where each combination's first costs have to be equal to or less than the capital available. In this case, mutually exclusive combinations will usually be realized, where selection of one group of independent alternatives will preclude the selection of another. This can be due to alternatives being in more than one group and/or capital limitations.

We will see that ranking alternatives according to their IRR values is not consistent with the PW, FW, or AW rankings. Mutually exclusive alternatives may be analyzed by incremental IRR analysis, and the results will be found to be completely consistent with the PW, FW, and AW methods. Incremental analysis assumes that we start with a satisfactory low-investment alternative. Analysis of a higher-investment alternative is then based on the differences between the cash flows of the second alternative and the acceptable alternative. These differences in cash flows are incremental cash flows. The cash flow of the second alternative is equal to the cash flow of the first alternative plus the incremental cash flows. Thus, if the incremental cash flow is acceptable when compared to the MARR, then the larger investment has to be a better investment than the first alternative, which was also acceptable.

Otherwise, remove the larger investment from consideration. This type of evaluation is continued until all alternatives have been evaluated; one of the mutually exclusive alternatives is then determined to be the best investment. As mentioned earlier, there is a possibility that the PW equation may be a polynomial in terms of i such that multiple roots i^* of polynomial $PW(i')$ may result. Often, multiple i^* 's are assumed to be multiple IRR values. This is misleading since there is really only one true IRR for an investment, and so we will need to determine which i^* , if any, is the investment IRR. Classifying investments into simple and nonsimple investments will tell us if just one i^* exists which, in turn, tells us that we have found the IRR when we have found i^* . An investment is simple if there is only one cash flow sign change (minus to plus) from period to period.:

D. RATES OF RETURN METHOD

The rate of return is a percentage that indicates the relative yield on different uses of capital. Three rates of return appear frequently in engineering economy studies:

- The minimum acceptable rate of return (MARR) is the rate set by an organization to designate the lowest level of return that makes an investment acceptable.
- The internal rate of return (IRR) is the rate on the unrecovered balance of the investment in a situation where the terminal balance is zero. It is a discount rate at which $NPV = 0$.
- The external rate of return (ERR) is the rate of return that is possible to obtain for an investment under current economic conditions. For example, suppose that analysis of an investment shows that it will realize an IRR of 50 percent. Rationally, it is not reasonable to expect that we can invest in the external market and get that high a rate. In engineering economy studies, the external interest rate most often will be set to the MARR.

MINIMUM ACCEPTABLE RATE OF RETURN

The minimum acceptable rate of return, also known as the minimum attractive rate of return, is a lower limit for investment acceptability set by organizations or individuals. It is a device designed to make the best possible use of a limited resource, i.e., money. Rates vary widely according to the type of organization, and they vary even within the organization. Historically, government agencies and regulated public utilities have utilized lower required rates of return than have 'competitive industrial enterprises. Within a given enterprise, the required rate may be different for various divisions or activities. These variations usually reflect the risk involved. For instance, the rate of return required for cost reduction proposals may be lower than that required for research and development projects in which there is less certainty about prospective cash flows.

INTERNAL RATE OF RETURN

The IRR is the best-known and most widely used rate-of-return method. It is also known as the true rate-of-return method and the discounted cash flow method. The internal rate of return, represented by i in the traditional interpretation of interest rates, is the rate of interest earned by an alternative investment on the unrecovered balance of an investment.

The internal rate of return can be calculated by equating the annual, present, or future worth of cash flow to zero and solving for the interest rate (IRR) that allows the equality, it should be added that solving for the interest rate in this manner results in a polynomial equation that is a function of i , which may result in multiple roots of the equation (). In such cases the IRR may or may not be one of the equation roots.

Although both the EAW and FW approaches are legitimate, the rate of return is often defined in terms of present worth, under the constraints of possible i^* roots, where the IRR is

- The interest rate at which the present worth of the cash flow of a project is zero, or, to restate this in another way:
- The rate which when employed in computing the present worth of all costs and present worths of all returns will make them equal

Because rate-of-return computations usually begin with a problem expressed in terms of present worth or annual worth, it is necessary to pay attention to the guidelines for the EAW and PW methods. In particular, mutually exclusive alternatives (where selection of one precludes selection of others) must be compared on the basis of equivalent outcomes. In the case of independent alternatives (the choice of one does not affect the choice of another, except for limited capital availability), all costs and benefits must be explicitly stated.

Calculation of IRR

Determining the IRR is a function of the type of investment (simple, pure, and mixed) and the characteristics of the alternatives (mutually exclusive or independent). If we have independent projects, we may fund combinations of the projects since an independent project does not affect the funding of another project (except for capital availability limitations which are very real in most situations analyzed by the engineering economist). The cash flows of several independent alternatives that are being considered as a group may be summed to form the group's composite cash flow. Analysis can then be performed on this composite cash flow. Where capital limitations are apparent in a department and several independent alternatives are competing for funding, combinations of alternatives may be formed where each combination's first costs have to be equal to or less than the capital available. In this case, mutually exclusive combinations will usually be realized, where

selection of one group of independent alternatives will preclude the selection of another. This can be due to alternatives being in more than one group and/or capital limitations.

We will see that ranking alternatives according to their IRR values is not consistent with the PW, FW, or AW rankings. Mutually exclusive alternatives may be analyzed by incremental IRR analysis, and the results will be found to be completely consistent with the PW, FW, and AW methods. Incremental analysis assumes that we start with a satisfactory low-investment alternative. Analysis of a higher-investment alternative is then based on the differences between the cash flows of the second alternative and the acceptable alternative. These differences in cash flows are incremental cash flows. The cash flow of the second alternative is equal to the cash flow of the first alternative plus the incremental cash flows. Thus, if the incremental cash flow is acceptable when compared to the MARR, then the larger investment has to be a better investment than the first alternative, which was also acceptable. Otherwise, remove the larger investment from consideration. This type of evaluation is continued until all alternatives have been evaluated; one of the mutually exclusive alternatives is then determined to be the best investment. As mentioned earlier, there is a possibility that the PW equation may be a polynomial in terms of i such that multiple roots i^* of polynomial $PW(i')$ may result. Often, multiple i^* 's are assumed to be multiple IRR values. This is misleading since there is really only one true IRR for an investment, and so we will need to determine which i^* , if any, is the investment IRR. Classifying investments into simple and nonsimple investments will tell us if just one i^* exists which, in turn, tells us that we have found the IRR when we have found i^* . An investment is simple if there is only one cash flow sign change (minus to plus) from period to period. A simple investment is as follows:

Time period	Cash flow (Rs.)	Sign change
Time period	Cash flow (Rs.)	Sign change

Cost Benefit Analysis

The question to which cost benefit analysis addresses itself is whether it is socially desirable to undertake a number of investment project A, B, C, D etc, and if investible funds are limited, then how many of these should be selected. Since the choice involves maximization, we have to discuss what it is that investment planners wish to maximize. In general terms an investment planners wants to maximize the present value of all benefits less that of all costs, subject to specific constraints. This general formulation raises the following specific questions, the answer to which provide the general principles of cost benefit analysis.

- In project appraisal which costs and which benefits are to be considered?
- How are these costs and benefits to be valued?
- How can profitability of a project be measured?
- What is the relevance of uncertainty in project appraisal?
- What are the relevant constraints?

There is certainty some arbitrariness in the choice of these questions.

In evaluating alternatives of private organizations, the criterion is to select the alternative with the maximum profit. The profit maximization is the main goal of private organizations while providing goods/services as per specifications to their customers. But the same criterion cannot be used while

evaluating public alternatives. Examples of some public alternatives are constructing bridges, roads, dams, establishing public utilities, etc.

The main objective of any public alternative is to provide goods/services to the public at the minimum cost. In this process, one should see whether the benefits of the public activity are at least equal to its costs. If yes, then the public activity can be undertaken for implementation. Otherwise, it can be cancelled. This is nothing but taking a decision based on Benefit-Cost ratio (BC) given by

$$BC\ ratio = \frac{\text{Equivalent benefits}}{\text{Equivalent costs}}$$

The benefits may occur at different time periods of the public activity. For the purpose of comparison, these are to be converted into a common time base (present worth or future worth or annual equivalent). Similarly, the costs consist of initial investment and yearly operation and maintenance cost. These are to be converted to a common time base as done in the equivalent benefits. Now the ratio between the equivalent benefits and equivalent costs is known as the "Benefit-Cost ratio". If this ratio is at least one, the public activity is justified; otherwise, it is not justified. Let

B_P - present worth of the total benefits

B_F = future worth of the total benefits

B_A = annual equivalent of the total benefits

P = initial investment

P_F = future worth of the initial investment

P_A = annual equivalent of the initial investment

C = yearly cost of operation and maintenance

C_P = present worth of yearly cost of operation and maintenance

C_F - future worth of yearly cost of operation and maintenance

$$BC\ ratio = \frac{B_P}{P + C_P} + \frac{B_F}{P_F + C_F} + \frac{B_A}{P_A + C}$$

EXAMPLES 1.1

EXAMPLE-1 In a particular locality of a state, the vehicle users take a roundabout route to reach certain places because of the presence of a river. This results in excessive travel time and increased fuel cost. So, the state government is planning to construct a bridge across the river. The estimated initial investment for constructing the bridge is Rs. 40,00,000. The estimated life of the bridge is 15 years. The annual operation and maintenance cost is Rs. 1,50,000. The value of fuel savings due to the construction of the bridge is Rs. 6,00,000 in the first year and it increases by Rs. 50,000 every year thereafter till the end of the life of the bridge. Check whether the project is justified based on BC ratio by assuming an interest rate of 12%, compounded annually.

Solution

Initial investment = Rs. 40,00,000

Annual operation and maintenance = Rs. 1,50,000

Annual fuel savings during the first year = Rs. 6,00,000

Equal increment in fuel savings in the following years = Rs. 50,000

Life of the project = 15 years

Interest rate = 12%

6,00,000 + 7,00,000

The cash flow diagram of the project is shown in Fig-1.1

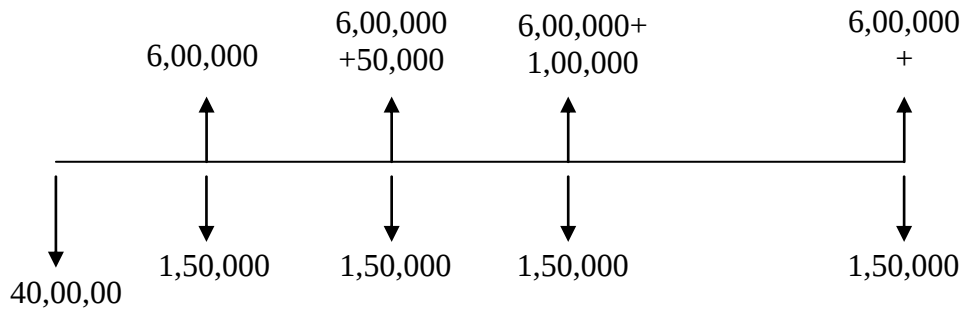


Fig-1.1 Cash flow diagram for constructing bridge.

Total present worth of costs = Initial investment (P)

+ Present worth of annual operating and maintenance cost (C_P) = $P + C_P$

= Rs. 40,00,000 + 1,50,000 $\times$ (P/A, 12%, 15)

= Rs. 40,00,000 + 1,50,000 $\times$ 6.8109

= Rs. 50,21,635

Total present worth of fuel savings (B_P):

A_1 = Rs. 6,00,000

G = Rs. 50,000

n - 15 years

i = 12%

Annual equivalent fuel savings (A) = $A_1 + G(A/G, 12\%, 15)$

= 6,00,000 + 50,000 (4.9803)

= Rs. 8,49,015

Present worth of the fuel savings (B_P) = $A(P/A, 12\%, 15)$

= 8,49,015 (6.8109)

= Rs. 57,82,556

$$BC \text{ ratio} = \frac{B_P}{P + C_P} + \frac{57,82,556}{50,21,635} = 1.1515$$

Since the BC ratio is more than 1, the construction of the bridge across the river is justified.

DEPRECIATION ANALYSIS

Depreciation is the decrease in value of physical properties with the passage of time and use. Most assets are worthless as they age. Production equipment gradually becomes less valuable through wear and tear. This lessening in value is recognised in accounting practices as an operating expense. Instead of charging the full purchase price of a new asset as one time expense, the outlay is spread over the life of the asset in the accounting records. Annual depreciation deductions are intended to match the yearly fraction of value used by an asset in the production of income over the asset's actual economic life. The actual amount of depreciation can never be established until the asset is retired from service.

Depreciation can be defined in three senses like physical depreciation, which is caused due to physical decay. Economic depreciation is the loss of value of an asset due to outdated technology and in accounting sense depreciation is the estimated value of fall in the worth of an asset. In accounting, depreciation charge is included in the cost of production of the asset. Depreciation is a permanent continuing and gradual shrinkage in the book value of a fixed asset.

Causes of depreciation:

Assets depreciate its value for several reasons.

1. Physical depreciation

Depreciation resulting in physical impairment of an asset is known as physical depreciation. This type of depreciation results in the lowering of the ability of a physical asset to render its intended service. The primary causes of physical depreciation are (a) deterioration due to action of the elements

including the corrosion of pipe, the rotting of timbers, chemical decomposition and so on. (b) Wear and tear charges (c) Physical decay, (d) Time factors etc.

2. Functional depreciation

Functional depreciation results not from a deterioration in the assets ability to serve its intended purpose, but from a change in the demand for the services it can render. The demand for the services of an asset may change it is more profitable to use a more efficient, unit, there is no longer work for the asset to do, or the work to be done exceeds the capacity of the asset.

3. Technological depreciation

Due to advancement of new technology, the old technology becomes outdated, so it loses its value. Obsolescence resulting from the discovery of another asset that is sufficiently superior to make it uneconomical to continue using the original asset. Assets also become obsolete when they are no longer needed.

4. Depreciation due to accident

Sometimes due to accident or sudden failure the asset loses its technological characteristic inherent in it.

5. Depreciation due to depletion

Consumption of an exhaustible natural resources to produce product or services is termed as depletion. Removal of oil, timber, rock or minerals from a site decreases the value of the holding. This decrease is compensated by a proportionate reduction in earnings derived from the resources.

6. Monetary depreciation

A change in the price level also decreases the value of owned assets. If prices rise during the life of an asset, then comparable replacement become more expensive. This means that the capital recovered will be insufficient to provide an adequate substitute for the worn out asset.

7. Depreciation due to time factor

There are some assets, which loses its values after a particular time period. Particularly the assets having lease, copyrights and patents right loses its value after the time is over.

8. Depreciation due to deferred maintenance

Sometimes the loss of value of asset begin very quickly due to deferred maintenance. If proper materials are not used or instructions to operate the machine are not properly obeyed the loss of value start.

9. Depreciation Accounting

Before going through the different method involved in the calculation of depreciation we should have sufficient knowledge about the depreciable property. Depreciable property is that property which can amortized or depreciated. Depreciable property may be tangible and intangible. Tangible property is any property that can be seen or touched. Intangible property are property which are not tangible like copyrights and patent rights. Depreciable tangible property is of two types i.e. Real and personal. Personal property are those property which is not real estate, they are machinery and equipments. Real property is land and anything that is erected on. Land is never depreciable.

Property is depreciable if it fulfills the following requirements:

- a) The property must be used in business or help to produce income

- b) The property must be something that wears out, decays, deteriorates, becomes obsolete, or loses value from natural causes.
- c) It must have determinable life and that life must be longer than 1 year.

In general, if property does not fulfill the above conditions can't be regarded as depreciable property.

Depreciation Methods

There are various depreciation methods that have evolved from time to time but there are three basic methods to understand the various calculation of depreciation schedules that are presently, in effect, it is first necessary to become acquainted with the three methods on which the current schedules are based. Some current depreciation schedules are based on straight line depreciation and others are based on a combination of straight line depreciation and declining balance depreciation.

Before going to discuss the basic methods and other methods of depreciation we should know some additional terms for clear understanding of the problem.

P = Purchase price (unadjusted basis) of assets. (This is the initial cost of acquiring an asset (purchase price + sales taxes) including transportation expenses.

S = Salvage value or future value at end of asset's life. It is the expected selling price of a property when the asset can no longer be used by its owner.

N = useful (tax) life of asset - The expected period of time that a property will be used in a trade or business or to produce income.

N = number of years of depreciation

Dt (n) = Annual depreciation charges.

Bt(n) = Book value shown on accounting records at end of year. It is the original cost, basis of the property, including any adjustment.

$Bt(0)=p$

Straight line method

The most widely used and simplest method for the calculation of depreciation is straight line method. The straight line method assumes that the value of an asset decreases at a constant rate. Thus if an asset has a first cost of Rs.5,000

and an estimated salvage value of Rs.500, the total depreciation and over its life will be Rs. 4,500. If the estimated life in 5 years, the depreciation per year will be $4,500 \div 5 = 900$. This is equivalent to a depreciation rate of $1 \div 5 = 20\%$ per year.

General expression for the calculation of depreciation and book value may be developed for the straight line method.

The depreciation in any year is $Dt = \frac{P - F}{n}$

General expression for the straight line method

End of year	Depreciation charge	Book value at end of year
0	-	P
1	$\frac{P - F}{n}$	$P - \left(\frac{P - F}{n} \right)$
2	$\frac{P - F}{n}$	$P - 2 \left(\frac{P - F}{n} \right)$
3	$\frac{P - F}{n}$	$P - 3 \left(\frac{P - F}{n} \right)$

End of year	Depreciation charge	Book value at end of year
N	$\frac{P - F}{n}$	$P - t \left(\frac{P - F}{n} \right)$
N	$\frac{P - F}{n}$	$P - n \left(\frac{P - F}{n} \right)$

The book value is $Bt = P - t \left(\frac{P - F}{n} \right)$ and the depreciation rate per year is $\frac{1}{n}$

Example: From the following data find out

- The depreciation charge during year 1

- b) The depreciation charge during year 2
- c) The depreciation reserve accumulated by the end of year 3
- d) The book value at the end of year 3

Initial cost of the asset = Rs. 5000

Life time = 5 years

Salvage value = 0

The cost of capital 5%

Solution

(a) & (b) In case of straight line method as the depreciation charge is constant, the depreciation charges for year 1 and 2 is constant.

$$Dt(1) = Dt(2) = \frac{P - F}{n} = \frac{5000}{5} = 1000 \text{ per year}$$

(c) The depreciation reserve at the end of the third year is the sum of the annual depreciation charges for the first three years and is equal to 3 (1000) = Rs. 3000

$$(d) \text{ The book value at the end of third year is } = 5000 - 3 \left(\frac{5000}{5} \right) = 2000$$

$$Bt(3) = 5000 - 3000 = \text{Rs. } 2000$$

Declining balance Method

Value of an asset diminishes at a decreasing rate. The declining balance depreciation assumes that an asset decreases in value-faster early rather than in the latter portion of its service life. By this method a fixed percentage is multiplied times the book value the asset at the beginning of the year to determine the depreciation charge for that year. Thus as the book value of the asset decreases through time, so does the size of the depreciation charge.

For example - First cost Rs. 5,000 Salvage value =Rs.1000

life of the asset five year, Depreciation rate 30% per year.

Declining Balance method

End of year	Depreciation charge during year	Bank value at end of year Rs.
0		5000
1	$(0.30) (50000) = 1,500$	3,1500
2	$(0.30) (3,500) = 1,050$	2,450
3	$(0.30) (2,450) = 735$	1,715
4	$(0.30) (1,7115) = 515$	1,200
5	$(0.30) (1,200) = 360$	840

For a depreciation rate a , the general relationship expressing the depreciation charge in any year for declining balance depreciation is:

$$D_{(t)} = a \cdot BV_{(t-1)}$$

We know book value

$$BV_{(t)} = B_{t-1} - Dt$$

Therefore, declining-balance depreciation.

$$B_{(t)} = B_{t-1} - a \cdot B_{t-1}$$

Using this recursive expression, we can determine the general expression for the depreciation charge and the book value for any point of time. These calculations are shown in the table.

$$D_{(t)} = a(1-a)^{t-1} P$$

$$\text{and the book value } BV_{(t)} = (1 - R) P$$

$$BV_{(t)} = P(1-a)^t$$

General expression for the declining balance method of depreciation

End of year	Depreciation charge during year	Book value at end of year
0	-	P
1	$a \times B_0 = a (P)$	$(1-a) B_0 = (1-a) P$
2	$a \times B_1 = a (1-R) P$	$(1-a) B_1 = (1-a)^2 P$
3	$a \times B_2 = a (1-R)^2 P$	$(1-a) B_2 = (1-a)^3 P$
T	$a \times B_{t-1} = a (1-R)^{t-1} P$	$(1-a) B_{t-1} = (1-a)^t P$

N	$a \times B_{t-1} = a (1-R)^{n-1} P$	$(1-a) B_{n-1} = (1-a)^n P$
---	--------------------------------------	-----------------------------

If the declining balance method of depreciation is used for income tax purposes the maximum rate that may be used is double the straight line rate that would be allowed to a particular asset a group of asset being depreciated. Thus for an asset with an estimated life of N years the maximum rate that may be used with this method is $R = 2/N$. Many firms and individuals choose to depreciate their assets using declining balance depreciation with the maximum allowable rate. Such a depreciation method is commonly known as the Double Declining Balance method of depreciation.

MODULE III COMMERCIAL BANKING

MEANING AND FUNCTIONS OF BANK

Meaning of Bank

A bank is an institution which deals with money and credit. It accepts deposits from the public, makes the funds available to those who need them, and helps in the remittance of money from one place to another. In fact, a modern bank performs such a variety of functions that it is difficult to give a precise and general definition of it. It is because of this reason that different economists give different definitions of the bank.

According to Crowther, a Bank “collects money from those who have it to spare or who are saving it out of their incomes, and it lends this money to those who require it.” In the words of Kinley, “A bank is an establishment which makes to individuals such advances of money as may be required and safely made, and to which individuals entrust money when not required by them for use.” According to John Paget, “No body can be a banker who does

not (i) take deposit accounts, (ii) take current accounts, (iii) issue and pay cheques, and (iv) collects cheques-crossed and uncrossed-for its customers.”

Prof. Sayers defines the terms bank and banking distinctly. He defines a bank as “an institution whose debts (bank deposits) are widely accepted in settlement of other people’s debts to each other.” Again, according to Sayers, “Ordinary banking business consists cash for bank deposits and bank deposits for cash; transferring bank deposits from one person or corporation to another; giving bank deposits in exchange for bills of exchange, government bonds, the secured promises of businessmen to repay and so forth”. According to the Indian Companies Act, 1949, banking means “the accepting for the purpose of Indian Companies lending or investment, of deposits of money from the public, repayable on demand or otherwise, and withdrawable by cheque, draft or otherwise.”

In short, the term bank in the modern times refers to an institution having the following features :

- i) It deals with money ; it accepts deposits and advances loans.
- ii) It also deals with credit; it has the ability to create credit, i.e., the ability to expand its liabilities as a multiple of its reserves.
- iii) It is commercial institution ; it aims at earning profit.
- iv) It is a unique financial institution that creates demand deposits which serve as a medium of exchange and, as a result, the banks manage the payment system of the country.

Functions of Commercial Banks or Modern Banks

In the modern world, banks perform such a variety of functions that it is not possible to make an all-inclusive list of their functions and services. However, some basic functions performed by the banks are discussed below.

1. Accepting Deposits. The first important function of a bank is to accept deposits from those who can save but cannot profitably utilise this saving themselves. People consider it more rational to deposit their savings in a bank because by doing so they, on the one hand, earn interest, and on the other, avoid the danger of theft. To attract savings from all sorts of individuals, the banks maintain different types of accounts :

(i) Fixed Deposit Account. Money in these accounts is deposited for fixed period of time (say one, two, or five years) and cannot be withdrawn before the expiry of that period. The rate of interest on this account is higher than that on other types of deposits. The longer the period, the higher will be the rate of interest. Fixed deposits are also called time deposits or time liabilities.

(ii) Current Deposit Account. These accounts are generally maintained by the traders and businessmen who have to make a number of payments every day. Money from these accounts can be withdrawn in as many times and in as much amount as desired by the depositors. Normally, no interest is paid on these accounts. Rather, the depositors have to pay certain incidental charges to the bank for the services rendered by it. Current deposits are also called demand deposits or demand liabilities.

(iii) Saving Deposit Account. The aim of these accounts is to encourage and mobilise small savings of the public. Certain restrictions are imposed on the depositors regarding the number of withdrawals and the amount to be withdrawn in a given period. Cheque facility is provided to the depositors. Rate of interest paid on these deposits is low as compared to that on fixed deposits.

(iv) Recurring Deposit Account. The purpose of these accounts is to encourage regular savings by the public, particularly by the fixed income group. Generally money in these accounts is deposited in monthly instalments for a fixed period and is repaid to the depositors along with

interest on maturity. The rate of interest on these deposits is nearly the same as on fixed deposits.

(v) Home Safe Account. Home safe account is another scheme aiming at promoting saving habits among the people. Under this scheme a safe is supplied to the depositor to keep it at home and to put his small savings in it. Periodical, the safe is taken to the bank where the amount of safe is credited to his account.

2. Advancing of loans. The second important function of a bank is advancing of loans to the public. After keeping certain cash reserves, the banks lend their deposits to the needy borrowers. Before advancing loans, the banks satisfy themselves about the creditworthiness of the borrowers. Various types of loans granted by the banks are discussed below:

(i) Money at Call. Such loans are very short period loans and can be called back by the bank at a very short notice of say one day to fourteen days. These loans are generally made to other banks or financial institutions.

(ii) Cash Credit. It is a type of loan which is given to the borrower against his current assets, such as shares, stocks, bonds, etc. Such loans are not based on personal security. The bank opens the account in the name of the borrowers and allows him to withdraw borrowed money from time to time upto a certain limit as determined by the value of his current assets. Interest is charged only on the amount actually withdrawn from the account.

(iii) Overdraft. Sometimes, the bank provides .overdraft facilities to its customers though which they are allowed to withdraw more than their deposits. Interest is charged from the customers on the overdrawn amount.

(iv) Discounting of Bills of Exchange. This is another popular type of lending by the modern banks. Through this method, a holder of a bill of exchange can get it discounted by the bank. In a bill of exchange the debtor accepts the bill drawn upon him by the creditor (i.e, holder of the bill) and agrees to pay (he amount mentioned on maturity. After making some

marginal deductions (in the form of commission), the bank pays the value of the bill to the holder. When the bill of exchange matures, the bank gets its payment from the party which had accepted the bill. Thus, such a loan is self-liquidating.

(v) Term Loans. The banks have also started advancing medium-term and long-term loans. The maturity period for such loans is more than one year. The amount sanctioned is either paid or credited to the account of the borrower. The interest is charged on the entire amount of the loan and the loan is repaid either on maturity or in installments.

3. Credit Creation. A unique function of the bank is to create credit. In fact, credit creation is the natural outcome of the process of advancing loan as adopted by the banks. When a bank advances a loan to its customer, it does not lend cash but opens an account in the borrower's name and credits the amount of loan to this account. Thus, whenever a bank grants a loan, it creates an equal amount of bank deposit. Creation of such deposits is called credit creation which results in a net increase in the money stock of the economy. Banks have the ability to create credit many times more than their deposits and this ability of multiple credit creation depends upon the cash-reserve ratio of the banks.

4. Promoting Cheque System. Banks also render a very useful medium of exchange in the form of cheques. Through a cheque, the depositor directs the bankers to make payment to the payee. Cheque is the most developed credit instrument in the money market. In the modern business transactions, cheques have become much more convenient method of settling debts than the use of cash.

5. Agency Functions. Banks also perform certain agency functions for and on behalf of their customers :

(i) Remittance of Funds. Banks help their customers in transferring funds from one place to another through cheques, drafts, etc.

(ii) Collection and Payment of Credit Instruments. Banks collect and pay various credit instruments like cheques, bills of exchange, promissory notes, etc.

(iii) Execution of Standing Orders. Banks execute the standing instructions of their customers for making various periodic payments. They pay subscriptions, rents, insurance premia, etc. on behalf of their customers.

(iv) Purchasing and Sale of Securities. Banks undertake purchase and sale of various securities like shares, stocks, bonds, debentures etc. on behalf of their customers. Banks neither give any advice to their customers regarding these investments nor levy any charge on them for their service, but simply perform the function of a broker.

(v) Collection of Dividends on Shares. Banks collect dividends, interest on shares and debentures of their customers.

(vi) Income Tax Consultancy. Banks may also employ income-tax experts to prepare income-tax returns for their customers and to help them to get refund of income-tax.

(vii) Acting as Trustee and Executor. Banks preserve the wills of their customers and execute them after their death.

(viii) Acting as Representative and Correspondent. Sometimes the banks act as representatives and correspondents of their customers. They get passports, traveller's tickets, book vehicles, plots for their customers and receive letters on their behalf.

6. General Utility Function. In addition to agency services, the modern banks provide many general utility services as given below:

(i) Locker Facility. Banks provide locker facility to their customers. The customers can keep their valuables and important documents in these lockers for safe custody.

(ii) Traveller's Cheques. Banks issue traveller's cheques to help their customers to travel without the fear of theft or loss of money. With this facility, the customers need not take the risk of carrying cash with them during their travels.

(iii) Letter of Credit. Letters of credit are issued by the banks to their customers certifying their creditworthiness. Letters of credit are very useful in foreign trade.

(iv) Collection of Statistics. Banks collect statistics giving important information relating to industry, trade and commerce, money and banking. They also publish journals and bulletins containing research articles on economic and financial matters.

(v) Underwriting Securities. Banks underwrite the securities issued by the government, public or private bodies. Because of its full faith in banks, the public will not hesitate in buying securities carrying the signatures of a bank.

(vi) Gift Cheques. Some banks issue cheques of various denominations (say of Rs.11, 21, 31, 51.101, etc.) to be used on auspicious occasions.

(vii) Acting as Referee. Banks may be referred for seeking information regarding the financial position, business reputation and respectability of their customers.

(viii) Foreign Exchange Business. Banks also deal in the business of foreign currencies. Again, they may finance foreign trade by discounting foreign bills of exchange.

ROLE OF COMMERCIAL BANKS IN A DEVELOPING ECONOMY

A well-developed banking system is a necessary pre-condition for economic development in a modern economy. Besides providing financial resources for the growth of industrialisation, banks can also influence the direction in which these resources are to be utilized. In the underdeveloped and developing countries, not only the banking facilities are limited to a few

developed urban areas, but also the banking activities are limited mostly to trade and commerce, paying little attention to industry and agriculture. Structural as well as functional reforms in the banking system are needed to enable the banks perform developmental role in underdeveloped countries.

Banks and Economic Development.

In a modern economy, banks are to be considered not merely as dealers in money but also the leaders in development. They are not only the store houses of the country's wealth but also are the reservoirs of resources necessary for economic development. Banks play an important role in the development of a country. It is the growth of commercial banking in the 18th and 19th centuries that facilitated the occurrence of industrial revolution in Europe. Similarly, the economic progress in the present day developing economies largely depends upon the growth of sound banking system in these economies. Commercial banks can contribute to a country's economic development in the following way.

1. Capital Formation. Capital formation is the most important determinant of economic development and banks promote capital formation. Capital formation has three well-defined stages: (a) generation of saving, (b) mobilisation of saving, and (c) canalisation of saving in productive uses. Banks play a crucial role in all the three stages of capital formation : (a) They stimulate savings by providing a number of incentives to the savers, such as, interest on deposits, free and cheap remittance of funds, safe custody of valuables, etc. (b) By expanding their branches in different areas and giving various incentives, they succeed in mobilizing the savings generated in the economy. They not only mobilise resources from those who have excess of them, but also make the resources so mobilized available to those who have the opportunities of productive investment.

2. Encouragement to Entrepreneurial Innovations. In underdeveloped countries, entrepreneurs generally hesitate to invest in new ventures and undertake innovations largely due to lack of funds. Facilities of bank loans enable the entrepreneurs to step up their investment and innovational activities, adopt new methods of production and increase productive capacity of the economy.

3. Monetisation of Economy. Monetisation of the economy is essential for accelerating trade and economic activity. Banks, which are creators and distributors of money, allow money to play an active role in the economy. They help the process of monetisation in two ways : (a) They monetise debts. In other words, they buy debts (i.e., securities which are not acceptable as money) and, in exchange, create demand deposits (which are acceptable as money), (b) By spreading their branches in the rural and backward areas, the banks convert the non-monetised sectors of the economy into monetised sectors.

4. Influencing Economic Activity. Banks can directly influence economic activity, and hence, the pace of economic development through its influence on (a) the rate of interest, and (ft) the availability of credit.

(i) Variations in Interest Rates. A reduction in the interest rates makes the investment more profitable and stimulates economic activity. An increase in the interest rate, on the other hand, discourages investment and economic activity. Thus, to overcome a deflationary situation, banks can follow cheap money policy with low interest rates and to control inflation they can adopt dear money policy with high interest rates.

(ii) Availability of Credit Bankers can also influe

Reserve Bank of India

government deposits, (b) It collects and makes payments on behalf of the government, (c) It helps the government to float new loans and manages the public debt, (d) It sells for the Central Government treasury bills of 91 days duration, (e) It makes 'Ways and Means' advances to the Central and State Governments for periods not exceeding three months, (f) It provides development finance to the government for carrying out five year plans, (g) It undertakes foreign exchange transactions on behalf of the Central Government, (h) It acts as the agent of the Government of India in the latter's dealings with the International Monetary Fund (IMF), the World Bank, and other international financial institutions, (i) It advises the government on all financial matters such as loan operations, investments, agricultural and industrial finance, banking, planning, economic development, etc.

3. Banker's Bank. The Reserve Bank acts as the banker's bank in the following respects : (a) Every Bank is under the statutory obligation to keep a certain minimum of cash reserves with the Reserve Bank. The purpose of these reserves is to enable the Reserve Bank to extend financial assistance to the scheduled banks in times of emergency and thus to act as the lender of the last resort. According to the Banking Regulation Act, 1949, all scheduled banks are required to maintain with the Reserve Bank minimum cash reserves of 5% of their demand liabilities and 2% of their time liabilities. The Reserve Bank (Amendment) Act, 1956 empowered the Reserve Bank to raise the cash reserve ratio to 20% in the case of demand deposits and. to 8% in case of time deposits. Due to the difficulty of classifying deposits into demand and time categories, the amendment to the Banking Regulation Act in September 1972 changed the provision of reserves to 3% of aggregate deposit liabilities, which can be raised to 15% if the Reserve Bank considers it necessary, (b) The Reserve Bank provide financial assistance to the scheduled banks by discounting their eligible bills and through loans and advances against

approved securities, (c) Under the Banking Regulation Act, 1949 and its various amendments, the Reserve Bank has been given extensive powers of supervision and control over the banking system. These regulatory powers relate to the licensing of banks and their branch expansion ; liquidity of assets of the banks ; management and methods of working of the banks ; amalgamation, reconstruction and liquidation of banks ; inspection of banks ; etc.

4. Custodian of Exchange Reserves. The Reserve Bank is the custodian of India's foreign exchange reserves. It maintains and stabilises the external value of the rupee, administers exchange controls and other restrictions imposed by the government, and manages the foreign exchange reserves. Initially, the stability of exchange rate was maintained through selling and purchasing sterling at fixed rates. But after India became a member of the international Monetary Fund (IMF) in 1947, the rupee was delinked with sterling and became a multilaterally convertible currency. Therefore the Reserve Bank now sells and buys foreign currencies, and not sterling alone, in order to achieve the objective of exchange stability. The Reserve Bank fixes the selling and buying rates of foreign currencies. All Indian remittances to foreign countries and foreign remittances to India are made through the Reserve Bank.

5. Controller of Credit. As the central bank of the country, the Reserve Bank undertakes the responsibility of controlling credit in order to ensure internal price stability and promote economic growth. Through this function, the Reserve Bank attempts to achieve price stability in the country and avoids inflationary and deflationary tendencies in the country. Price stability is essential for economic development. The Reserve Bank regulates the money supply in accordance with the changing requirements of the economy. The

Reserve Bank makes extensive use of various quantitative and qualitative techniques to effectively control and regulate credit in the country.

6. Ordinary Banking Functions. The Reserve Bank also performs various ordinary banking functions : (a), It accepts deposits from the central government, state governments and even private individuals without interest, (b) It buys, sells and rediscounts the bills of exchange and promissory notes of the scheduled banks without restrictions, (c) It grants loans and advances to the central government, state governments, local authorities, scheduled banks and state cooperative banks, repayable within 90 days, (d) It buys and sells securities of the Government of India and foreign securities, (e) It buys from and sells to the scheduled banks foreign exchange for a minimum amount of Rs. 1 lakh, (f) It can borrow from any scheduled bank in India or from any foreign bank, (g) It can open an account in the World Bank or in some foreign central bank, (h) It accepts valuables, securities, etc., for keeping them in safe custody, (i) It buys and sells gold and silver.

7. Miscellaneous Functions. In addition to central banking and ordinary banking functions, the Reserve Bank performs the following miscellaneous functions: (a) Banker's Training College has been set up to extend training facilities to supervisory staff of commercial banks. Arrangements have been made to impart training to the cooperative personnel, (b) The Reserve Bank collects and publishes statistical information relating to banking, finance, credit, currency, agricultural and industrial production, etc. It also publishes the results of various studies and review of economic situation of the country in its monthly bulletins and periodicals.

8. Forbidden Business. Being the central bank of the country, the Reserve Bank (a) should not compete with member banks and (b) should keep its assets in liquid form to meet any situation of economic crisis. Therefore, the

Reserve Bank has been forbidden to do certain types of business : (a) It can neither participate in, nor directly provide financial assistance to any business, trade or industry, (b) It can neither buy its own shares nor those of other banks or commercial and industrial undertakings, (c) It cannot grant unsecured loans and advances, (d) It cannot give loans against mortgage security, (e) It cannot give interest on deposits, (f) It cannot draw or accept bills not payable on demand, (g) It cannot purchase immovable property except for its own offices.

9. Promotional and Developmental Functions. Besides the traditional central banking functions, the Reserve Bank also performs a variety of promotional and developmental functions : (a) By encouraging the commercial banks to expand their branches in the semi-urban and rural areas, the Reserve Bank helps (i) to reduce the dependence of the people in these areas on the defective unorg

COSTING AND COST CONCEPTS

Cost accounting is recently used in every sphere of modern day business. Of course it has its origin from the ancient time. Of course the farmers and the craftsmen were using the technique to ascertain the cost of their product. But its real development has begun during the eighteenth and nineteenth century.

Cost accounting is accounting for cost. The cost accounting consists of two words: Cost and Accounting. Cost means the resources sacrificed for the production of a commodity and accounting refers to the financial information

system. Cost accounting system can be described as measurement and reporting of resources used in monetary terms. Cost accounting is the branch of accounting dealing with the classification, recording, allocation, summarisation and reporting of current and prospective cost.

Costing and cost accounting

We use costing and cost accounting interchangeably. But they should not be. We should know, what are the differences. Costing refers to the technique and process of ascertaining cost. The technique consists of the principles and rules for the determining the costs of products and services.

Cost accounting on the other hand, is defined as the process of accounting for cost from the point at which expenditure is incurred or committed. It is that specialised branch of accounting which involves classification, accumulation, allocation, absorption and control of costs.

The concept of cost accounting is some bit wider than costing and cost accounting. It includes several subjects like costing, cost accounting, cost control, budgetary control, and cost audit. According to CIMA, cost accounting is the application of costing and cost accounting principles, methods and techniques to the science, art and practice of cost control. It includes the presentation of information derived those from for the purpose of managerial decision making.

- a) Cost ascertainment: Ascertaining the cost of goods produced and services rendered has been the chief function of cost accounting. This purpose is some times referred to as product costing or cost accumulation,
- b) Cost Analysis: Cost analysis is one of the important function of cost accounting.' Because cost accounting helps in decision making. When

making decision, we require information about cost, revenue and other information, So we have to analyse the cost.

- c) Cost control: To control the cost, is the chief motive of every management. Cost information shows the performance of the organization. There are two types of cost control method: Standard Costing and Budgetary Control. Actual costs are compared on the budgeted cost. This help in controlling the cost.

Objectives of cost accounting

1. The cost accounting helps in ascertaining the cost of production of every units, job, operation process, department and service.
2. It indicate to management any inefficiency and the extent of various forms of waste, whether as material, time, expense or in the use of machine, equipment and tools.
3. It disclose profitable and unprofitable activities so that steps can be taken to eliminate or reduce those from what, little or no profit is obtained or to change the method of production or incidence of cost in order to render such activities more profitable.
4. It provides actual figures of cost for comparison with estimates and to
5. assist the management in their price fixing policy.
6. It present comparative cost data for different periods and different volumes of production and those by assist the management in budgetary control.
7. It record and report to the concerned manager how actual costs compare with standard cost and possible causes of differences between them.
8. It indicates the exact cause of increase or decrease in profit or loss shown by the financial accounts.
9. It also provides data for comparison cost within the firm and also between similar firm.

COST CONCEPTS

Cost form the subject matter of cost accounting. Cost are the resources sacrificed to achieve a specific objective. It is defined as the benefit sacrificed to serve some benefit.

Cost classification

Proper classification of cost is necessary for the clear understanding of the cost.

The cost can be classified according to their common characteristics. The classification may be:

1. Behavioural classification
2. Direct and indirect cost
3. Product cost and period cost
4. Relevant and irrelevant cost
5. Real cost
6. Opportunity cost

Behavioural classification

The behavioural classification shows how the cost behaves when production change. According to behavioral classification, there are three types of cost, fixed cost, variable and semi-variable cost.

Fixed costs

Fixed cost is independent of output. Whatever may the output, they remain constant. They are generally time-based. Some typical examples are rent, insurance, taxes, salaries etc. Fixed cost is of two types, committed fixed cost and discretionary fixed cost. The shape of fixed cost curve is presented below:

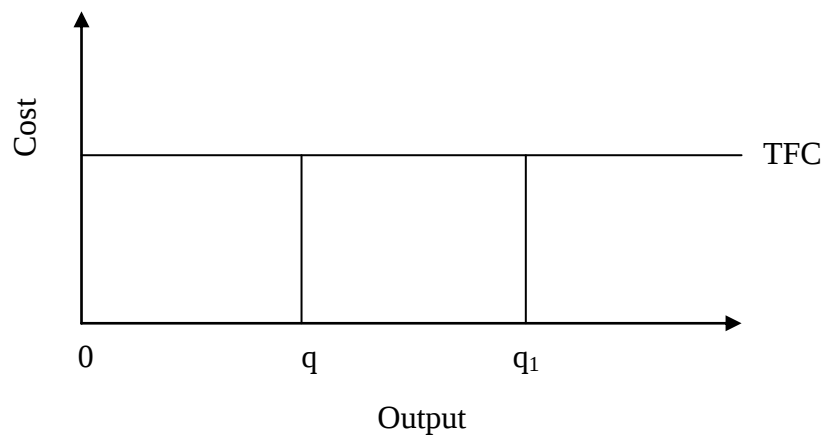


Fig. 1

VARIABLE COSTS

It may be defined as a cost which in the aggregate, tends to vary in direct proportion to changes in the volume-of output or turn-over within relevant range for a given budget period. Examples of variable costs are material costs, direct labour costs, sales commission, power, royalty, carriage, packing cost etc. As output increases variable costs increases in the same proportion. Thus, we can say that there exist a linear relationship between output volume and variable costs. Consequently, variable costs are constant per unit of output. Hence, total variable costs curve is a straight line passing through the origin and average variable costs curve is a horizontal line.

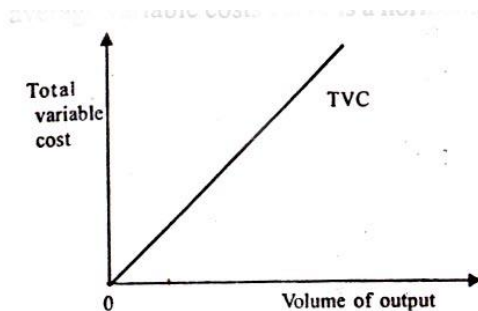


Fig. 2

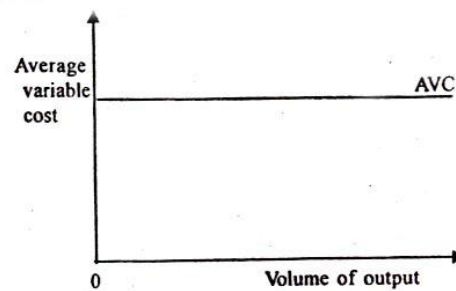


Fig. 3

Very often variable costs are called engineered costs because these have an explicit, specified, physical relationship with a selected measure of activity. Direct material and "direct labour are a prime example of engineered cost. An engineered variable cost is said to exist when work measurement techniques (material standards with the help of production engineers, labour standards through time and motion study) have carefully established an optimum relationship between input and output. The implication for the management in planning and controlling of variable costs is that with all other factors held constant, each desired per unit expansion of productive activity triggers an incremental change in total variable costs equal to a constant amount per unit.

SEMI VARIABLE COSTS

The behavior of cost can't be expected to remain as fixed or variable under all circumstances and for all the time spans. Thus, the concept of semi-variable cost may arise. Semi-variable costs stand mid-way between fixed and variable costs. Semi-variable cost is defined as a cost containing both fixed and variable elements, and which is thus, partly affected by fluctuations in the level of activity. The fixed part of a semi-variable cost usually represents a minimum fee for making a particular item/service available. The variable portion is the cost charges for actually using the service. For example, most telephone service charges are made up of two elements :

- i. a fixed charge for allowing to make a call,
- ii. plus an additional variable charge for each call actually made.

Semi-variable costs are also known as mixed costs as they consist both of fixed costs and variable costs. The first part is not affected by the changes in volume of production, while the later part is sensitive to changes in the volume of production. Thus, semi-variable costs change in the same directions as volume but not in direct proportion thereto. Hence, the shape of semi-variable cost curve is as shown below :

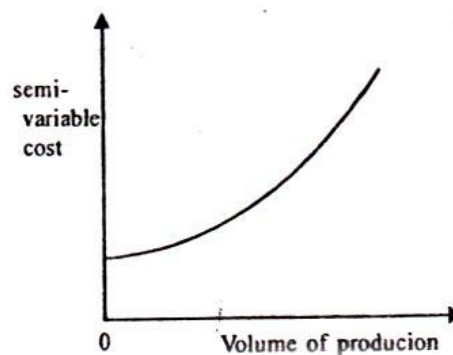


Fig. 4

Marshall has made broad division of cost as fixed cost and variable cost. Variable costs are known as the prime costs. Marshall's variable costs include the costs of raw materials, wages of the labourers and wear and tear charge of machineries used for the purpose. Prime cost is called Variable cost because it directly varies with the rate of production. Higher is the level of production, more is the level of output, greater will be the amount of variable cost, Lower is the level of production, lower is the volume of output lower will be, the variable cost. It is called prime cost because this is the main cost of production. In any factory or firm if we analyse the cost of production the amount of variable cost constitutes the three-fourth of the costs of production. Therefore, it is primary or main cost of production.

Fixed costs are those costs which are independent of output may be more or less or even zero, fixed costs are incurred. Costs of the machineries, buildings, salaries of the staff, maintenance of the machine, costs of telephone, wages of watch man. Insurance fee or administrative expenses are the example of fixed cost. These costs are incurred whatever may be the size of output. These costs are incurred before the factory starts production and after the factory closes down its production for some times. These fixed costs are payment for the fixed factors of production. Fixed costs are supplementary costs because these costs constitute a small portion of the total costs of production. These costs are also called as the overhead costs of production, because these costs decline per unit of output with increase in production and increase per unit output with decrease in production.

The difference or distinction between the variable and fixed costs is not rigid. It is one of degrees not of kind. To take an example the wage paid to a typist is called fixed costs. If the services of the typist is permanent it becomes a fixed costs. If the services of the typist can be terminated when production

stops this will be variable cost. Therefore, distinction is of degrees and only found in the short-run. In the long run- every cost is a variable costs.

Average Cost and Marginal Cost :

Average cost per unit of output is nothing.

$$\frac{\text{but the total cost}}{\text{Number of commodities produced}}$$

Mathematically speaking. (Average cost) = $\frac{TC}{TO}$

For example, if the total cost of producing 100 units of output, is Rs. 1000/-.

Then average cost =

is equal to $\frac{TC-100}{TO=100}$ = Rs. 10/- AC

Total cost consists of two types of costs such as fixed cost and variable cost. Corresponding to that we can have average fixed cost and average variable cost.

Average fixed cost $AFC = \frac{TFC}{TO}$

AVC (Average variable cost) = $\frac{TVC}{TO}$

Therefore average cost is equal to average fixed cost and average variable cost.

Marginal Cost:

Marginal cost is the cost of producing an additional unit of output. That is a net addition to the total cost. Marginal cost is the difference between the total cost of producing any number of commodity minus the total cost of producing one units less than the number. If the number is N the marginal cost or (MC) = The total cost of producing N units of commodity TC_N minus the total cost of production one units less i.e. TC_{N-1} . So marginal cost (MC) $TC_N - TC_{N-1}$.

This can be illustrated with the help of an arithmetic example. Suppose, the total cost of producing 103 units of commodity is 1000 rupees and the total cost of producing 101 units of commodity is 1020 rupees. Here the marginal cost $MC = TC = (1020 - TC_{n-1})$ i.e. Rs.-1000/-=20.

Marginal cost is associated with variable cost. It is no way connected with fixed cost Because there is no addition to the fixed cost when the additional units of commodity ' ' is produced,, marginal cost is independent of fixed cost. Producing one more units causes nothing to be added to the fixed cost. Whether fixed cost is 1000/- dollar or 10,000 dollar marginal cost is unaffected.

COST OF PRODUCTION OF A FIRM

Units of out put	Total fixed costs	Total variable cost	Total cost (2+3)	Average fixed cost (2+1)	Average variable cost (3+1)	Average cost (5+6)	Marginal cost
1	2	3	4	5	6	7	8
1.	100	100	200	100	100	200	200
2.	100	150	250	50	75	125	50
3.	100	200	300	33.3	66.7	100	50
4.	100	260	360	25	65	90	60
5.	100	320	420	20	64	84	60
6.	100	410	510	16.6	86.4	85	90
7.	100	503	603	14.3	71.7	86	93
8.	100	652	752	12.5	81.5	94	149
9.	100	827	927	11.1	91.9	103	175
10.	100	1035	1135	10	103.5	113.5	208

Direct cost and indirect cost

Direct costs are directly identified with a product, process or department. Raw materials used and labour employed in manufacturing an article are common example of direct costs.

Indirect costs- These costs are not applicable any particular product process or department but are common to different products. Factory manager's salary, factory rent, depreciation of machinery are typical example of indirect cost.

Relevant cost and irrelevant cost

Relevant cost are the cost which are relevant for decision making such as differential or incremental cost, opportunity costs, out of pockets costs etc.

Irrelevant cost

Irrelevant costs are those which are not pertinent to a decision. These are the costs that will not be changed by a decision because irrelevant cost will not be affected, they may be ignored in decision making process.

Product cost and period cost

Product costs are the cost directly identified with the product. These are the cost of goods produced and kept ready for sale. They are direct materials, direct labour, variable factory overheads. Periods costs are those cost which are not directly related with production of the commodity. It is otherwise known as fixed cost.

Direct cost

→	Direct Material	(Ex. Primary packing materials)
→	Direct Labour	(Ex. Wages paid to workers)
→	Direct Expenses cost of excise duty, royalties, insurance	(Ex. Cost of special tools, patterns etc.) hire charges of a special equipment etc.

Indirect Cost

→	Indirect Material work, Small tools)	(Ex. Fuel, Lubricating oil, Maintenance
→	Indirect Labour inspectors, workshop	(Ex. Wages of general supervisors, cleaners, store keeper, time-keeper etc.)
→	Indirect Expenses hospital welfare	(Ex. Rent, lighting insurance, canteen, expenses, it is otherwise known as overhead expenses)

→	Factory/work overhead (Work manager's salary, factory rent, factory insurance, salaries of clerical & executive staff etc.)
→	Office & Administrative overhead (Office rent, office lighting, insurance etc.)
→	Selling & Distributive overhead (advertising expenses, salaries of salesman, indirect packing material etc.)

Real Cost of Production.

Though in our analysis producer is interested in money cost of producing commodity, another view of cost of production is known as real costs of production. Those who talk about the real cost of production they talk about the sacrifices borne by the society to produce a particular commodity, They hold the view that money costs to production is much less in comparison to the sacrifices made by the society to produce a particular commodity. To illustrate, we can consider the wage of a factory worker is not equal to the sacrifice he makes in terms of his mental and physical labour. He works under great risks. Nobody pays for it. Similarly in factory area, the air and water get polluted. Slums are created. It spreads diseases. Nobody pays for it. Growth of a factory brings indiscipline and conflict. Society sacrifices much. Nobody pays for this sacrifice. So from social stand Point cost of a commodity should be calculated in terms of sacrifices. Money cost does not give true picture of cost Marshall defines real costs as “The exertions of all the different kinds of labourers that are directly or indirectly involved in making it, together with the abstinence or rather the waiting’s required for raising the capital used in making it, all these efforts and sacrifices together will be called the costs of production of the commodity”.

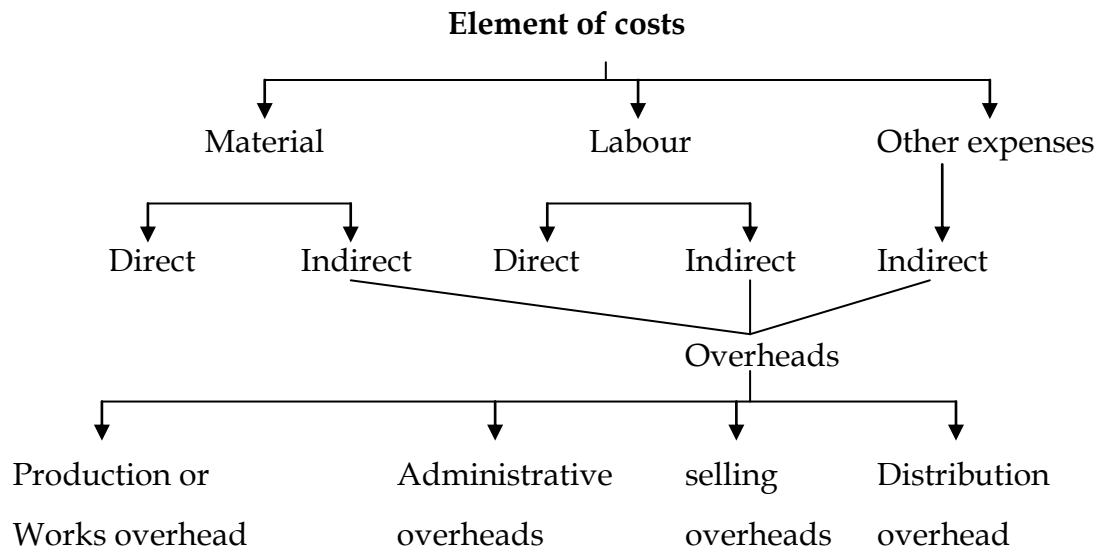
Marshall conceived the cost of production in terms of pains and sacrifices. The sacrifices made by labour to produce commodity, the sacrifices undertaken by-the savers to provide capital by reducing their consumption and all other social sacrifices required to produce a commodity constitute the cost of production of a commodity. These real costs give the true picture of cost of production which cannot be measured scientifically, because it involves sacrifices. Sacrifice is a subjective feeling. Its objective measurement is impossible. So people today are trying to make it objective by social cost benefit analysis. Therefore money costs of induction is accepted as the cost of production.

Opportunity Cost :

Modern writers view another concept to measure the Boney cost. This is known as opportunity or alternative cost. Opportunity cost is the cost of alternative foregone. It is grained that every factor of production has several uses, en we employ the factor for one use we forego the opportunity of employing it in another use. Resources or factors limited in supply. If we produce one commodity we do not produce another. Therefore, the opportunity cost of producing a commodity is equal to the cost of not producing another commodity. To take an example if we have an acre can produce potato on it and get 1000 rupees. Had we not produced potatoes and have produced rice on it we would have got 700 rupees. Therefore, the cost of load for producing potato would be equal to the alternative foregone that 700 rupees from rice productions. The second point to be noted about this it is not only the cost of the alternative foregone but also the cost of the best alternative foregone illustrate a film artist working as a nurse later become nursing teacher. When she was a nurse she was getting 6000 rupees of income per annum. When she become a nursing teacher she got 10.000 rupees per annum. Then she metered the film industry as a labourer. What will be her of production as a labour in the film industry? Then it will not be alternative foregone as a nurse but as the best native foregone as a nursing teacher. Then supply price at the cost of production will not be the Rs 6000 per annum but 10,000 rupees per annum. Therefore. Benham defines opportunity costs thus. "The opportunity cost of anything is the best alternative that could be produced by the same factor by an equivalent group of factors costing the same amount of money".

Element of costs

The total cost is analysed by elements of cost.



By grouping the above elements of cost the following given of costs are obtained.

- | | |
|---------------------------|---------------------------------------|
| a) Prime cost- | Direct material + Direct Labour |
| b) Works or factory cost- | Prime cost + works overhead |
| c) Cost of production- | Works cost + administrative overhead. |
| d) Total cost of sales- | Cost of production + selling and |
| Distribution | overheads. |
| e) Profit or loss- | Sales - Total cost. |

Example : Ascertain the prime cost, works cost, cost of production total cost and profit from the following information's.

Direct material = 7000

Direct Labour = 2,800

Factory expenses = 2,600

Administrative expenses = 1000

Selling expenses = 900

Sales = 20,000

Solution : Prime cost = Direct materials + Direct Labour
 = Rs. 7,000 + Rs. 2,800
 = Rs. 9,800

Work cost = Prime cost + Factory expenses
 = Rs. 9,000 + Rs. 2,600

	= Rs. 12,400
Cost of Production	= Works cost + Administrative expenses
	= Rs. 12,400 + Rs. 1000
	= Rs. 13,400
Total cost	= cost of production + selling expenses
	= Rs. 13,400 + Rs. 900
	= Rs. 14,300
Profit	= Sales - Total cost
	= Rs. 20,000 - 14,300
	= Rs. 5,700

Questions

- 1- Define costing? Explain the different classification of costing?
- 2- Distinguish between direct cost and indirect cost?
- 3- What is product costing? What are the different elements of costing?
- 4- Distinguish between fixed cost and variable cost with diagrams?
- 5- What do you mean by overhead? What is a cost sheet?
- 6- What do you mean by opportunity cost?

STRUCTURE OF INDIAN MONEY MARKET

Meaning

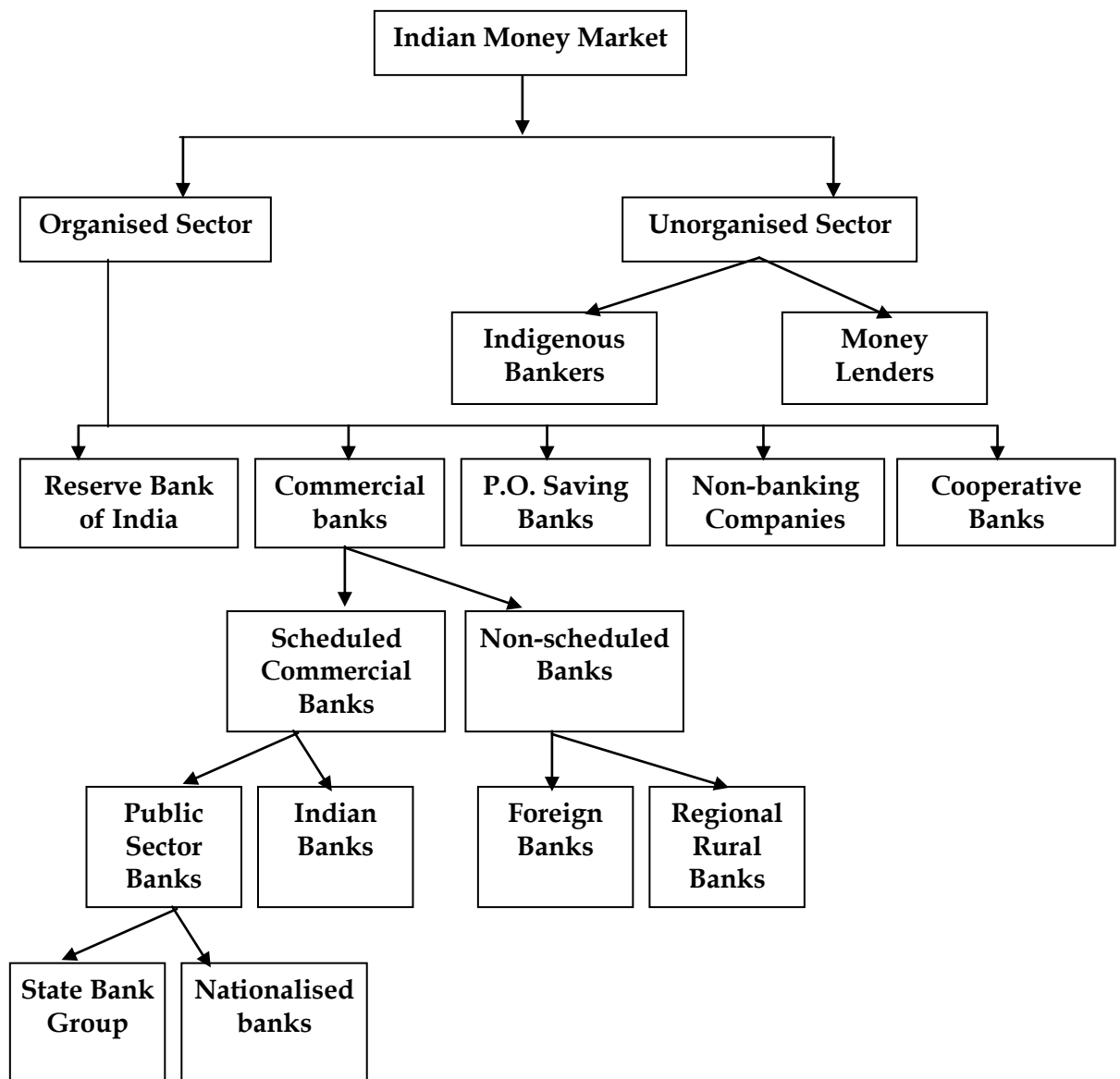
Financial markets are functionally classified into (a) money market and (b) capital market. This classification is on the basis of term of credit, i.e., whether the credit is supplied for a short period or long period. Money market refers to institutional arrangements which deal with short-term funds. Capital market, on the other hand, deals in long-term funds. Money market is a short-term credit market which deals with relatively liquid and quickly marketable assets, such as, short-term government securities, treasury bills, bills of exchange, etc. According to Crowther, "The money market is a collective name given to the various firms and institutions that deal with various grades of near-money." The Reserve Bank of India defines money market "as the centre for dealing, mainly of a short-term character, in money assets; it

meets the short-term requirements of borrowers and provides liquidity or cash to lenders.”

Structure of India Money market

- i) Broadly speaking the money market in India comprises two sectors (a) organized the money market in sectors: (b) organized sector.
- ii) The organized sector consists of the Reserve Bank of India, the State Bank of India with its seven associates, twenty nationalise” commercial banks, other schedule and non-scheduled commercial banks, foreign banks, and Regional Rural Banks. It is called organised because its part are systematically coordinated by the RBI.
- iii) Non-bank financial institutions such as the LIC, the GIC and subsidiaries, the UTI also operate in this market, but only indirectly through banks, and not directly.
- iv) Quasi-government bodies and large companies also make their short term surplus funds available to the organized marker through banks.

CHART 1
STRUCTURE OF INDIAN MONEY MARKET



- v) Cooperative credit institutions occupy the intermediary position between organized and unorganized parts of the Indian money market. These institutions have a three-tier structure. At the top there are state cooperative banks. At the local level, there are primary credit societies and urban cooperative banks. Considering the size method of operations, and dealings with the RBI and commercial banks, only state and central cooperative banks should be included in the organized sector. The cooperative societies at the local level are loosely linked with it.

Unorganised Sector of the Indian Money Market

The unorganized segment of the Indian money market is composed of unregulated non-bank financial intermediaries, indigenous bankers and money lenders which exist even in the small towns and big cities. Their lending activities are mostly restricted to small towns and villages. The persons who normally borrow from this unorganised sector include farmers, artisans small traders and small scale producers who do not have any access to modern banks. The following are some of the constituents of unorganised money market in India.

1. Indigenous Bankers : Indigenous bankers include those individuals and private firms which are engaged in receiving deposits and giving loans and thereby act like a mini bank. Their activities are not at all regulated. During the ancient and medieval periods, those indigenous bankers were very active. But with the growth of modern banking, particularly after the advent of British, the business of the indigenous bankers received a set back. Moreover, with the growth of commercial banks and Co-operative banks the area of operations of indigenous bankers has again contracted further. Even till today, a few thousands of indigenous bankers are still operating in the

western and southern parts of the country and engaged themselves in the traditional banking business.

2. Unregulated non-bank financial intermediaries : There are different types of unregulated non-bank financial intermediaries in India. They are mostly constituted by loan or finance companies, chit funds and 'nidhis'. A good number of finance companies in India are engaged in collecting substantial amount of funds in the form of deposits, borrowings and other receipts. They normally give loans to wholesale traders, retailers, artisans, and different self-employed persons at a high rate of interest ranging between 36 to 48 per cent. There are various types of chit funds in India. They are doing business in almost all the states but the major portion of their business is concentrated in Tamil Nadu and Kerala. Moreover, there are 'nidhis' operating in South India which are a kind of mutual benefit funds restricted to its members.

3. Money Lenders : Money lenders are advancing loans to small borrowers like marginal and small farmers, agricultural labourers, artisans, factory and mine workers, low paid staffs, small traders etc. at a very high rates of interest and also adopt various malpractices for manipulating loan records of these poor borrowers. There are broadly three types of money lenders: (i) professional money lenders dealing solely with money lending; (ii) itinerant money lenders such as Kabulis and Pathans and (iii) non professional money lenders. The area of operation of the money lenders is very much localised and their methods of operation is also not uniform. The money lending operation of the money lenders is totally unregulated and unsupervised which leads to worst exploitation of the small borrowers. The money lenders has become a necessary evil in the absence of sufficient institutional sources of credit to the poorer sections of society. Although various measures have been introduced to control the activities of money lenders but due to lack of

political will these are not enforced, leading to a huge exploitation of small borrowers.

Organised Sector of Indian Money Market

The organised segments of the Indian money market is composed of the Reserve bank of India (RBI), the State Bank of India, Commercial banks, Co-operative banks, foreign banks, finance corporations and the Discount and Finance House of India Limited. The segment of Indian money market is quite integrated and well organised. Mumbai, Calcutta, Chennai, Delhi, Bangalore and Ahmedabad are the leading centres of the organised sector of the Indian money market. The Mumbai money market is a well organised one, having the head offices of the RBI and different commercial banks, the leading well developed stock exchange, the bullion exchange and fairly organised market for Government securities. All these have placed the Mumbai money market at par with New York money market of USA and London money market of England. The main constituents of the organised sector of Indian money market include: (i) The Call Money Market, (ii) The Treasury Bill Market, (iii) The Commercial Bill Market, (iv) The certificates of Deposits Market, (v) Money Market for Mutual Funds and (vi) The Commercial Paper Market.

- (i) **The Call Money Market:** The call money market in a most common form of developed money market. It is a most sensitive segment of the financial system which reflects clearly any change in it. The call money market in India is very much centred at Mumbai, Chennai and Calcutta and out of which the Mumbai is the most important one. In such market, lending and borrowing operations are carried out for one day. The call money market is also termed as inter-bank call money market. Normally, scheduled commercial banks, Co-operative banks and the Discount and Finance House of India (DFHI) operate in this market and in a special situation, the LIC, UTI, the GIC, the IDBI and the NABARD are permitted

to operate as lenders in this call money market. In this market, brokers usually play an important role.

- (ii) **The Treasury Bill Market:** Treasury bill markets are markets for treasury bills. In India such treasury bill are short term liability of the Central Government which are of 91 day and 364 day duration. Normally, the treasury bills should be issued so as to meet temporary revenue deficit over expenditure of a Government at some point of time. But, in India, the treasury bills are, now a days, considered as a permanent source of funds for the Central Government. In India, the RBI is the major holders of the treasury bills, which is around 90 per cent of the total. In India, ad-hoc treasury bills have now been replaced by ways and means Advances since April 1, 1997, so as to finance temporary deficits of the Central Government.
- (iii) **The Commercial Bill Market:** The Commercial bill market is a kind of sub-market which normally deals with trade bills or the commercial bills. It is a kind of bill which is normally drawn by one merchant firm on the other and they arise out of commercial transactions. The purpose for issuing a commercial bill is simply to reimburse the seller as and when the buyer delays payment. But, in India, the commercial bill market is not so developed. This is mainly due to popularity of the cash credit system in bank lending and the unwillingness on the part of large buyer to bind himself to payment schedule related to the commercial bill and also the lack of uniform approach in drawing bills.
- (iv) **The Certificate of Deposit (CD) Market:** The certificate of Deposit (CD) was introduced in India by the RBI in, March 1989 with the sole objective of widening the range of money market instruments and also to attain higher flexibility in the development of short term surplus funds for the investors. Initially the CDs are issued by scheduled commercial banks in multiples of Rs. 25 lakh and also to the extent of a minimum of Rs. 1 crore. The maturity of CDs are varied between three months and one

year. In India, six financial institutions, viz., IDBI, ICICI, IFCI, IRBI, SIDBI and Export and Import Bank of India were permitted in 1993 to issue for period varying between 1 to 3 years. Banks normally pay high rates of interest on CDs. In 1995-96, the stringent conditions in the money market induced the bankers to mobilise a good amount of resources through CDs.

- (v) **The Commercial Paper Market:** In India, the Commercial Paper (CP) was introduced in the money market in January 1990. A listed company having working capital not less than Rs. 5 crore can issue CP. Again the CP can be issued in multiples of Rs. 25 lakhs subject to a minimum of Rs. 1 crore for a maturity period varying between three to six months.
- (vi) **Money Market Mutual Funds:** In India, the RBI has introduced a scheme of Money Market Mutual Funds (MMTFs) in April 1992. The main objective of this scheme was to arrange an additional short term avenue for the individual investors. This scheme has failed to receive much response as the initial guidelines were not attractive. Thus, in November, 1995, the RBI introduced some relaxations in order to make the scheme more attractive and flexible. As per the exiting guidelines, the banks, public financial institutions and the private financial institutions are allowed to set up MMMFs. In the mean time, the limits of investment in individual instruments by MMMF has already been deregulated.

The Indian money market has its distinctive characteristics as it suffers from various defects. The following are some of its characteristics:

1. Lack of adequate integration. There is lack of adequate integration in the Indian money market. The organised and the unorganised sector of Indian money market are totally separate from each other and they have independent financial operations of their own. Therefore, activities of one sector has no impact on the activities of the other sector. It is very difficult to

establish a national money market under such a background. However, the Mumbai money market has been emerging as a strong money market in recent times. Moreover, the various constituents of the Indian money market viz., commercial banks, Co-operative banks and foreign banks are competing among themselves and particularly, the competition is much in the countryside. Even the commercial banks are competing among themselves. Again, the monetary policy of the RBI is also not effective to maintain adequate integration among the various constituents of Indian money market.

2. Shortage of funds : Another important feature of Indian money market is the shortage of funds. Therefore, the demand for loanable funds in the money market is much higher than that of its supply. This shortage of fund is mostly resulted from - (i) small capacity to save arising out of low per capita income; (ii) inadequate banking network and poor banking habit of the people, in general; (iii) absence of adequate and diversified investment opportunities and finally, the emergence of strong parallel economy having a huge magnitude of black money. In recent years, the development of rural banking structure, with the opening rural branches of commercial banks and with the expansion of Co-operative banks, has improved the fund position of the Indian money market, to some extent.

3. Lack of adequate banking facilities: Indian money market is also characterised by lack of adequate banking facilities. Rural banking network in the country is still inadequate. Population per bank office in India was 12,000 persons in 1993 as compared to that of only 1,400 persons in USA. In the rural areas, a substantial number of population, having small saving potential, have no access to facilities. Under such a system, a huge amount of small savings are not mobilised which needs to be mobilised for its productive uses through the expansion of banking network.

4. Lack of rational interest rate structure : There is lack of rational interest structure which is mostly resulted from lack of co-ordination among different banking institutions. Recently, there is some improvement in this regard, particularly after the introduction of standardisation of interest rates by the RBI for its rationalisation. However, the present system of administered interest rates is suffering from the defects like - (i) too many concessional rates of interest ; (ii) comparatively low yield on government securities, and (iii) improper lending and deposit rates fixed by the commercial banks.

5. Absence of Organised Bill Market: There is absence of organised bill market in India although the commercial banks purchase and discount both inland and foreign bills to a limited extent. Although, the RBI has introduced its limited bill market under its scheme of 1952 and 1970, but the same scheme has failed to popularise the bill finance in India. The popularity of the cash credit system and lack of uniformity in commercial bills are mostly responsible for the poor development of bill market in the country. Even after the introduction of Bill Market Scheme, 1970, the bill finance has declined and its extent has declined from 20.3 per cent in 1971 to a mere 11.0 per cent in 1995-96.

6. Existence of Unorganised Money Market : Another important feature of Indian money market is the existence of its unorganised character, where one of its segment is constituted by the indigenous bankers and money lenders. This unorganised segment is completely separated from the organised segment of the money market. Although the RBI has tried to bring the indigenous bankers under its direct control but the attempts have failed. Thus, as the indigenous bankers remained outside the organised money market, therefore, RBI's control over the money market is quite limited.

7. Seasonal stringency of money and fluctuations in interest rates : Another important feature of Indian money market is its seasonal stringency of money

and the volatile fluctuation of interest rates. India, being a agricultural country has to face huge demand for funds during the period of October to June every year so as to meet its requirement for farm operations and. also for trading in agricultural produce. But the money market is not having sufficient elasticity thus it creates seasonal stringency of funds leading to a rise in the rate of interest. But in the rainy and slack season the demand for fund slumps down leading to an automatic fall in the rate of interest. Such regular fluctuations in interest rates are not at all conducive to developmental activities of the country.

Underdevelopment of Indian Money Market

Considering the various defects of Indian money market it can be observed that the money market in India is relatively under-developed. Moreover, in respect of resources, organisation stability and elasticity, the said market cannot be compared with the developed money markets of London and New York. But among the third world countries India has been maintaining the most developed banking system. Even then the organisation of the money market is still underdeveloped. The under development nature of Indian money market is mostly determined by the following shortcomings.

Firstly, Indian money market fails to possess an adequate and continuous supply of short term assets such as treasury bills, bills of exchange, short term Government bonds etc.

Secondly, this market is lacking the highly organised banking system, so important for the successful working of a money market.

Thirdly, the sub-markets like acceptance market and the commercial bill market are non-existent in Indian money market.

Fourthly, Indian money market has totally failed to develop market for short term assets and accordingly there are no dealers of short term assets who acts as intermediaries between the Government and the entire banking system.

Fifthly, Indian money market is suffering from lack of co-ordination between its different constituents.

Sixthly, Indian money market again fails to attract any foreign funds.

Finally, Indian money market cannot be termed as a developed one considering its supply of fund and the liquidity position. Measures to Reform and Strengthen Indian Money Market.

In recent years, serious efforts have been made by the Government and the RBI to remove the shortcomings of Indian money market. RBI, in the mean time has reduced considerably the differences between the various constituents of money market. Differences in the interest rates has also been reduced by the RBI and the monetary stringency has also been reduced by the RBI through open market operations and bill market scheme.

Even then! Indian money market is still very much dependent on the call money market which is again characterised by high volatility. In the mean time, the RBI has introduced various measures to reform the money market as per recommendations of the Sukhamay Chakraborty Committee on the "Review of the working of the Monetary system" and the Narasimham Committee report on the working of the Financial System in India. The following are some of the important reform measures introduced to strengthen the Indian money market:

- (i) **Remission of Stamp Duty :** In order to remove the major administrative constraint in the use of bill system, the Government has remitted the stamp duty in August 1989. However, the experts feel that unless the cash credit system is discouraged this government decision to remit the stamp duty is not going to favour the prevailing bill system.
- (ii) **Deregulation of interest rates :** Another important steps to strengthen the money market was to deregulate the money market interest rates since May, 1989. This will bring interest rate flexibility and transparency in money market transactions. Again in November, 1991, as per the recommendations of the Narasimham Committee, the interest rates have been further deregulated and the banks and other financial institutions have been advised to determine and adopt market related rates of interest as far as practicable.
- (iii) **Introduction of new instruments :** The RBI has introduced certain money market instruments for strengthening the market conditions. These instruments are- 182 days treasury bills, longer maturity treasury bills, certificates of Deposits (CDs) Commercial Paper (CP) and dated Government securities. Discount and Finance House of India (DFHI) promoted the 182-day treasury bills systematically and these bills were the first security sold by auction for financing the fiscal deficit of the Central Government Again, the DFHI has also developed a secondary market in these bills and they become popular with the commercial banks. Again in 1992-93, the Government decided to introduce 364 day treasury bills and discontinued the 164- day treasury bills. The 364 day treasury bills can be held by commercial banks for meeting its statutory liquidity ratio.
- (iv) **DFHI:** The Discount and Finance House of India (DFHI) was setup in April 25, 1988 as a part of the reform package for strengthening money market. The main function of DFHI is do bring the entire financial system consisting of the scheduled commercial banks, co-operative

banks, foreign banks and all- India financial institutions, both in the public and private sector, within the fold of the Indian money market. This House will normally buy bills and short term papers from different banks and financial institutions in order to invest all of their idle funds for short periods. DFHI has also started to buy and sell government securities from April 1992 in limited quantity with the necessary refinance support from the RBI.

- (v) **Money Market Mutual Funds (MMMFs) :** The Government announced the establishment of Money Market Mutual Funds (MMMFs) in April 1992 with the sole objective to bring money market instruments within the reach of individuals. The MMMFs have been set up by different scheduled commercial banks and public financial institutions. The shares or units of MMMFs has been issued only to individuals.

Thus the aforesaid measures to reform Indian money market has helped it to become more advanced, solvent and vibrant. With the introduction of new instruments, the secondary market has also been developed considerably. Moreover, with the setting up of DEHI and MMMFs, the lot of Indian money market has also achieved considerable progress in recent times and is also expected to achieve further progress in the years to come.